

History and Practice of Digital Sound Synthesis

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Overview



Outline

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- **Outline**
- CCRMA Perspective

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Digital sound synthesis approaches in approximate historical order:

- Wavetable (one period)
- Subtractive
- Additive
- Frequency Modulation (FM)
- Sampling
- Spectral Modeling
- Physical Modeling

Some connections with audio coding will be noted

Emphasis:

- Sound examples
- Block diagrams
- Historical notes



CCRMA Perspective

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The Knoll, Stanford University



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Early Digital Sound Synthesis



Wavetable Synthesis in Music I-V (1957-1969)

Overview

Early Digital Synthesis

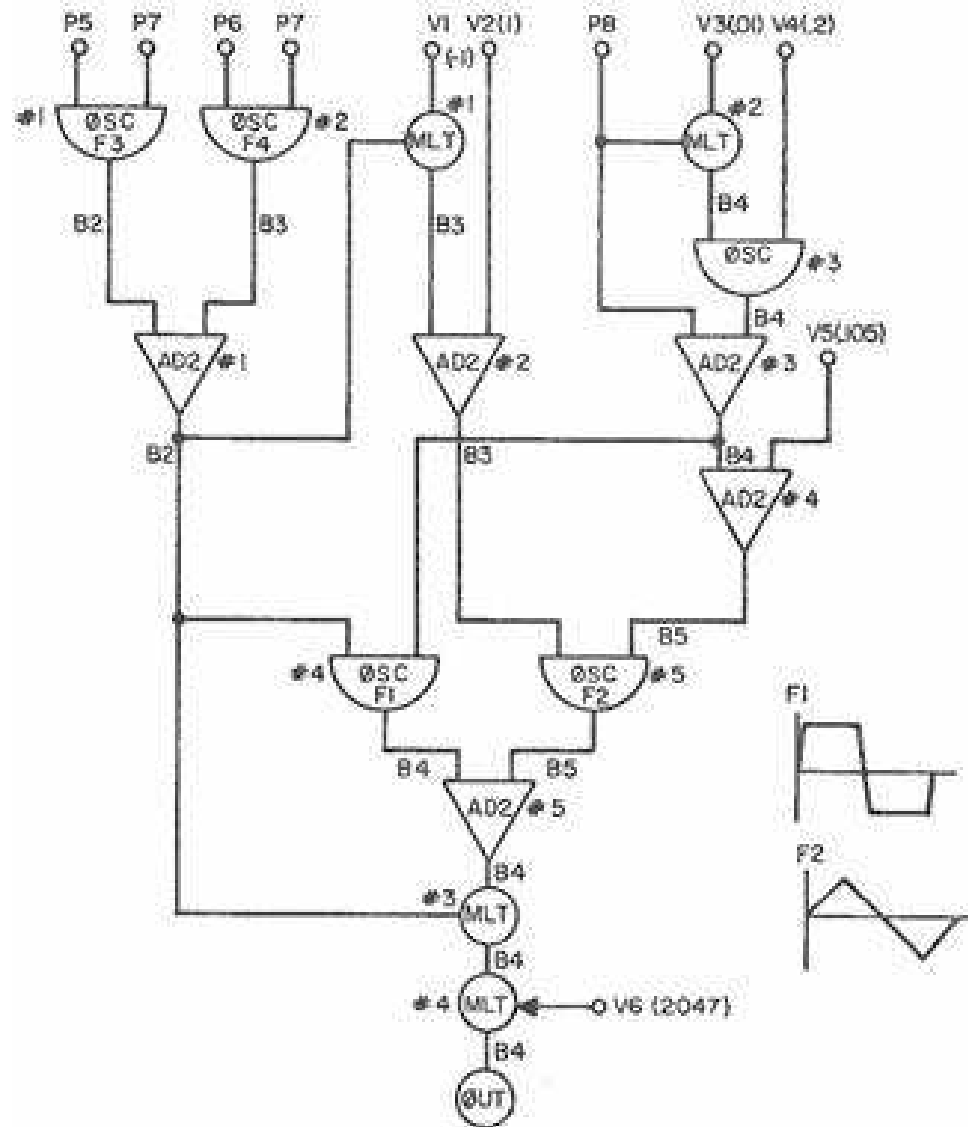
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Music V Scripting Language (“Note Cards”)

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```
INS 0 4 ;
ØSC P5 P7 B2 F3 P30 ;
ØSC P6 P7 B3 F4 P29 ;
AD2 B2 B3 B2 ;
MLT B2 V1 B3 ;
AD2 B3 V2 B3 ;
MLT P8 V3 B4 ;
ØSC B4 V4 B4 F5 P28 ;
AD2 P8 B4 B4 ;
AD2 B4 V5 B5 ;
ØSC B3 B5 B5 F2 V7 ;
ØSC B2 B4 B4 F1 V8 ;
MLT B2 B4 B4 ;
MLT B4 V6 B4 ;
ØUT B4 B1 ;
END ;
```

- Essentially Supported in MPEG-4 Structured Audio Orchestra Language (SAOL) (Music V → csound → SAOL)
- “Encoding sounds” as “instruments” is hard, in general



Kelly-Lochbaum Vocal Tract Model

Overview

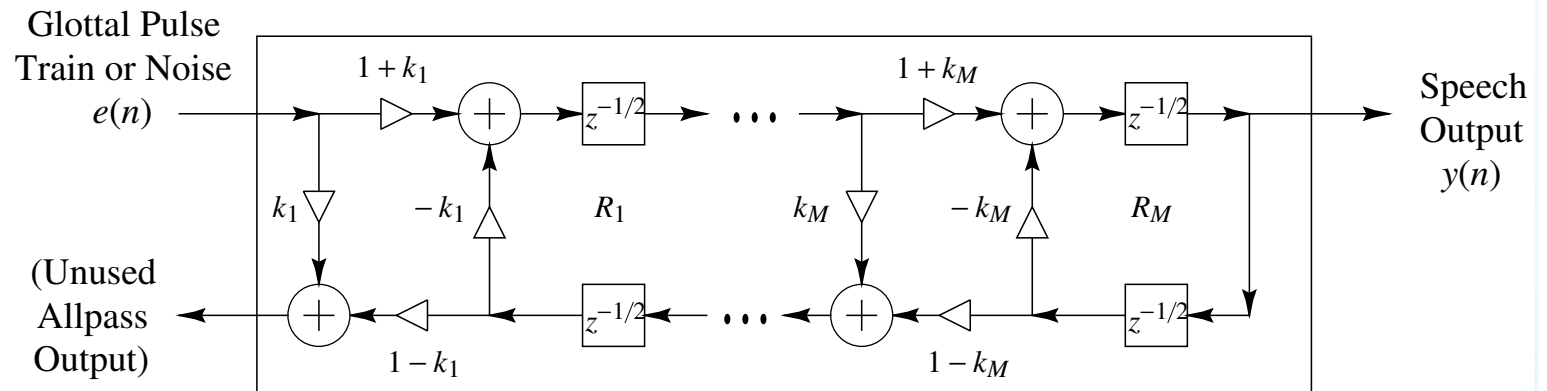
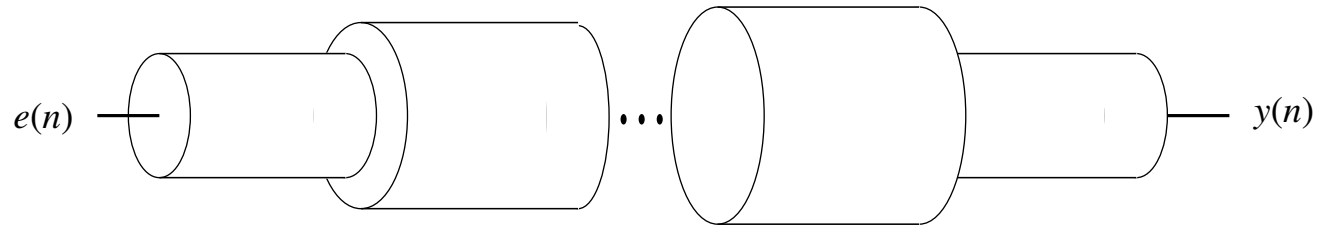
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Kelly-Lochbaum Vocal Tract Model (Piecewise Cylindrical)

John L. Kelly and Carol Lochbaum (1962)



Sound Example

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“Bicycle Built for Two”: (WAV) (MP3)

- Vocal part by Kelly and Lochbaum (1961)
- Musical accompaniment by Max Mathews
- Computed on an IBM 704
- Based on Russian speech-vowel data from Gunnar Fant’s book
- Probably the first digital physical-modeling synthesis sound example by any method
- Inspired Arthur C. Clarke to adapt it for “2001: A Space Odyssey” — the computer’s “first song”



Classic Additive-Synthesis Analysis (Heterodyne Comb)

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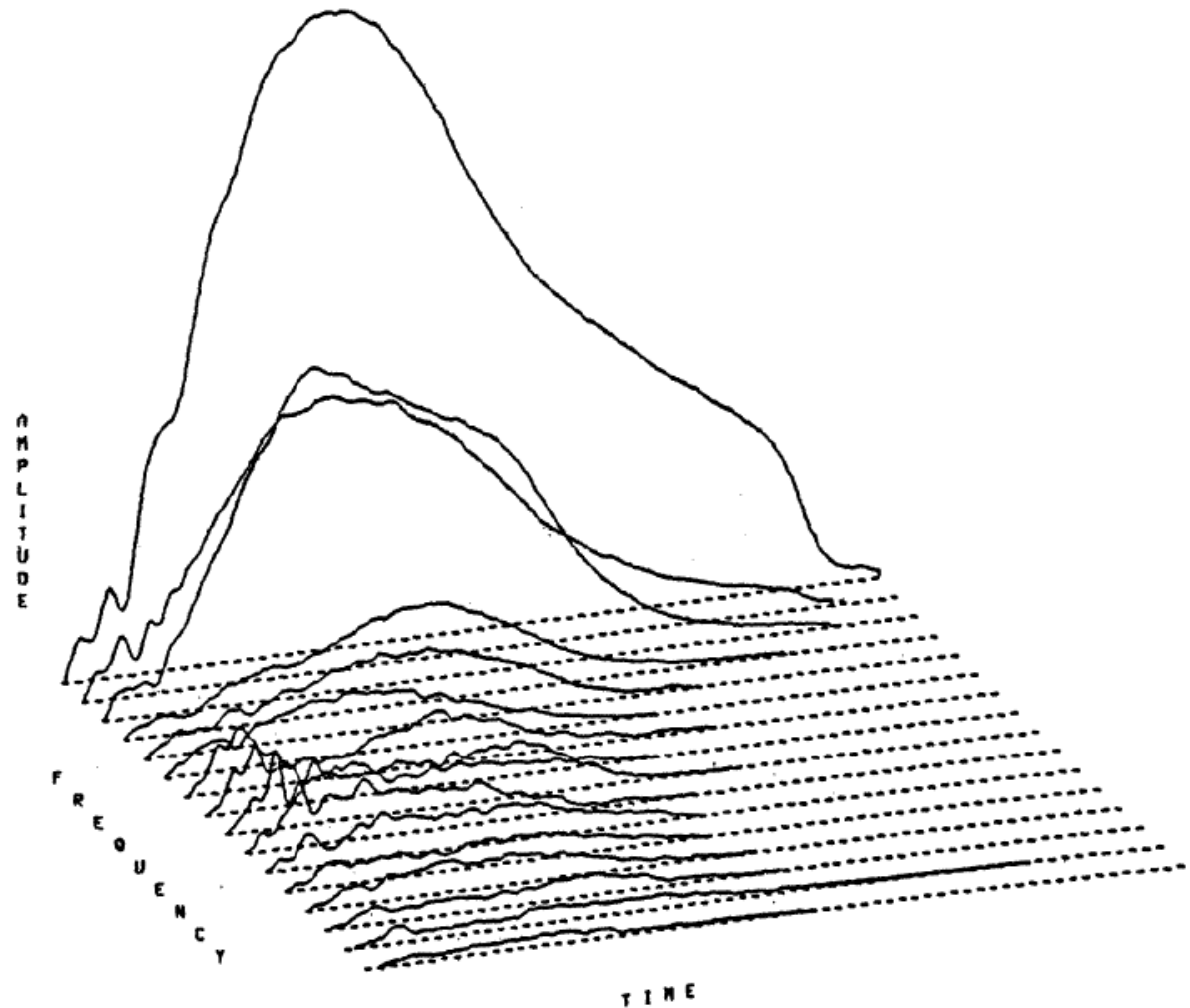
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John Grey 1975 — CCRMA Tech. Reports 1 & 2
(CCRMA “STANM” reports — available online)



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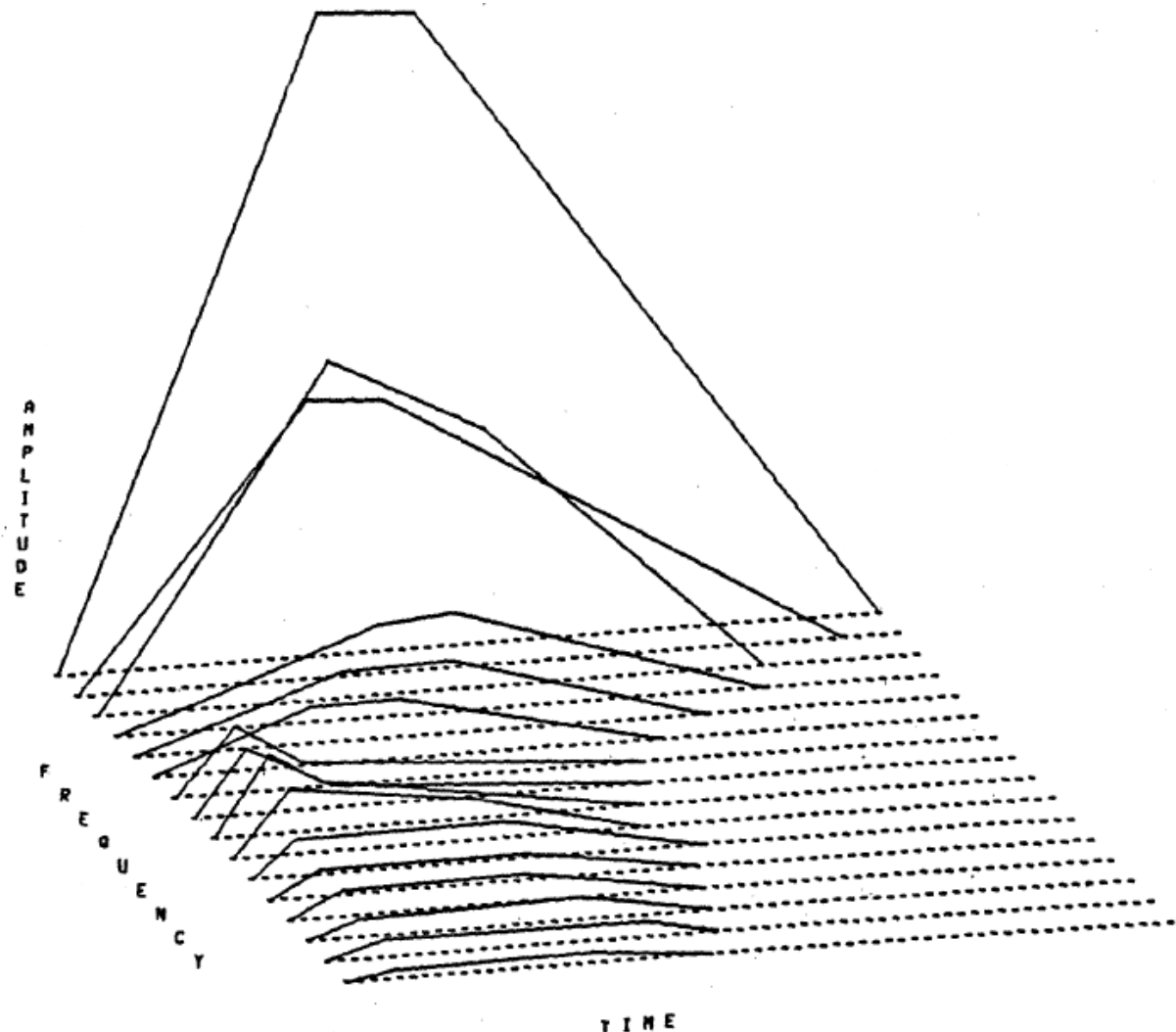
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Classic Additive-Synthesis (Sinusoidal Oscillator Envelopes)



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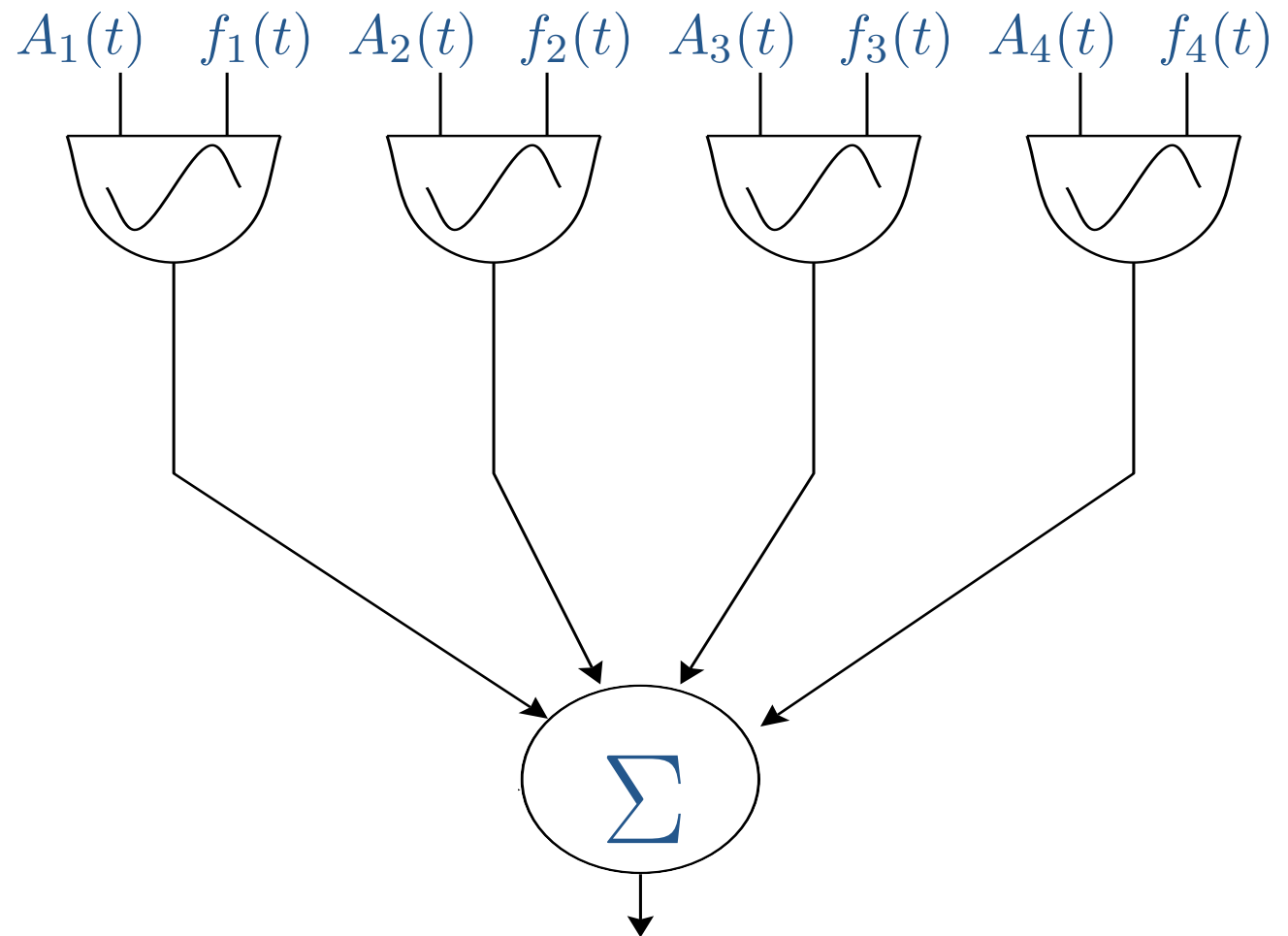
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Classic Additive Synthesis Diagram



$$y(t) = \sum_{i=1}^4 A_i(t) \sin \left[\int_0^t \omega_i(t) dt + \phi_i(0) \right]$$





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Classic Additive-Synthesis Examples

- Bb Clarinet
- Eb Clarinet
- Oboe
- Bassoon
- Tenor Saxophone
- Trumpet
- English Horn
- French Horn
- Flute
- All of the above
- Independently synthesized set

(Synthesized from original John Grey data)



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Frequency Modulation (FM) Synthesis

FM synthesis is normally used as a *spectral modeling* technique.

- Discovered and developed (1970s) by John M. Chowning (CCRMA Founding Director)
 - Key paper: JAES 1973 (vol. 21, no. 7)
 - Commercialized by Yamaha Corporation:
 - DX-7 synthesizer (1983)
 - OPL chipset (SoundBlaster PC sound card)
 - Cell phone ring tones
-
- On the physical modeling front, synthesis of vibrating-string waveforms using *finite differences* started around this time: Hiller & Ruiz, JAES 1971 (vol. 19, no. 6)



FM Formula

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$$x(t) = A_c \sin[\omega_c t + \phi_c + A_m \sin(\omega_m t + \phi_m)]$$

where

(A_c, ω_c, ϕ_c) specify the *carrier* sinusoid

(A_m, ω_m, ϕ_m) specify the *modulator* sinusoid

Can also be called *phase modulation*



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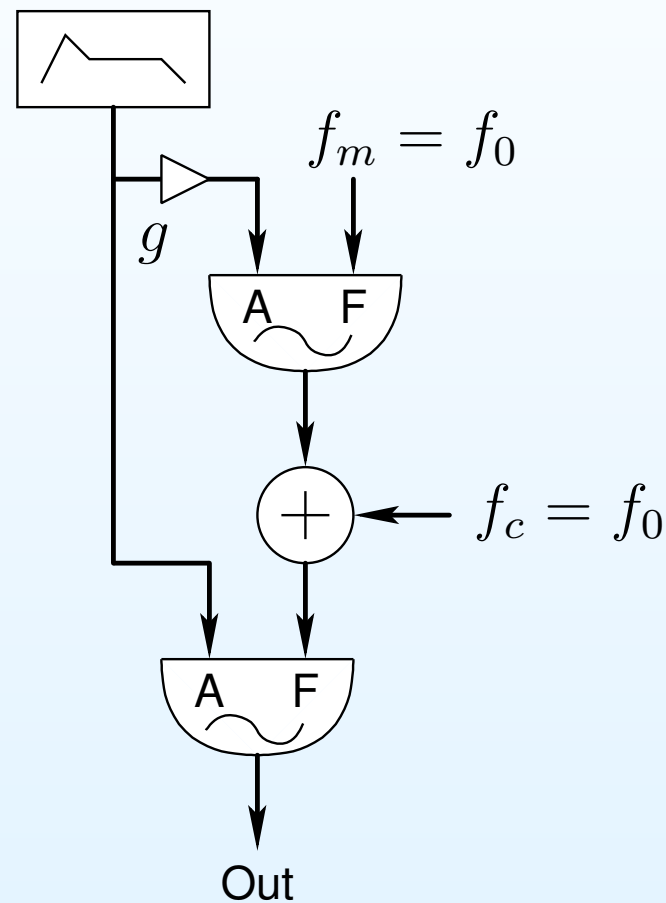
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Simple FM “Brass” Patch (1970–)

Jean-Claude Risset observation (1964–1969):
Brass bandwidth \propto amplitude





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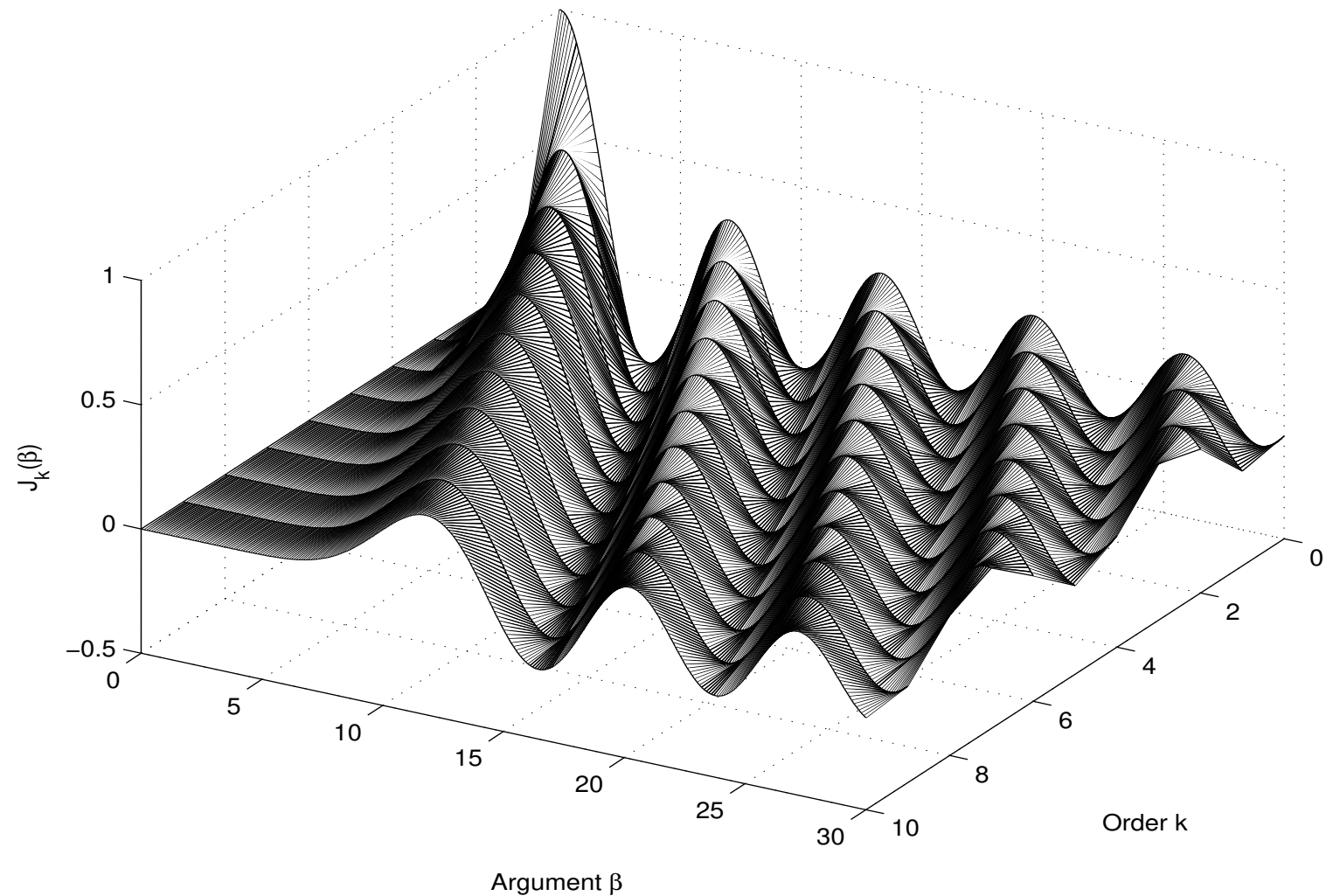
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FM Harmonic Amplitudes (Bessel Function of First Kind)

Harmonic number k , FM index β :





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Frequency Modulation (FM) Examples

All examples by John Chowning unless otherwise noted:

- FM brass synthesis
 - Low Brass example
 - Dexter Morrill’s FM Trumpet
- FM singing voice (1978)
Each formant synthesized using an FM operator pair (two sinusoidal oscillators)
 - Chorus
 - Voices
 - Basso Profundo
- Other early FM synthesis
 - Clicks and Drums
 - Big Bell
 - String Canon



FM Voice

Overview

Early Digital Synthesis

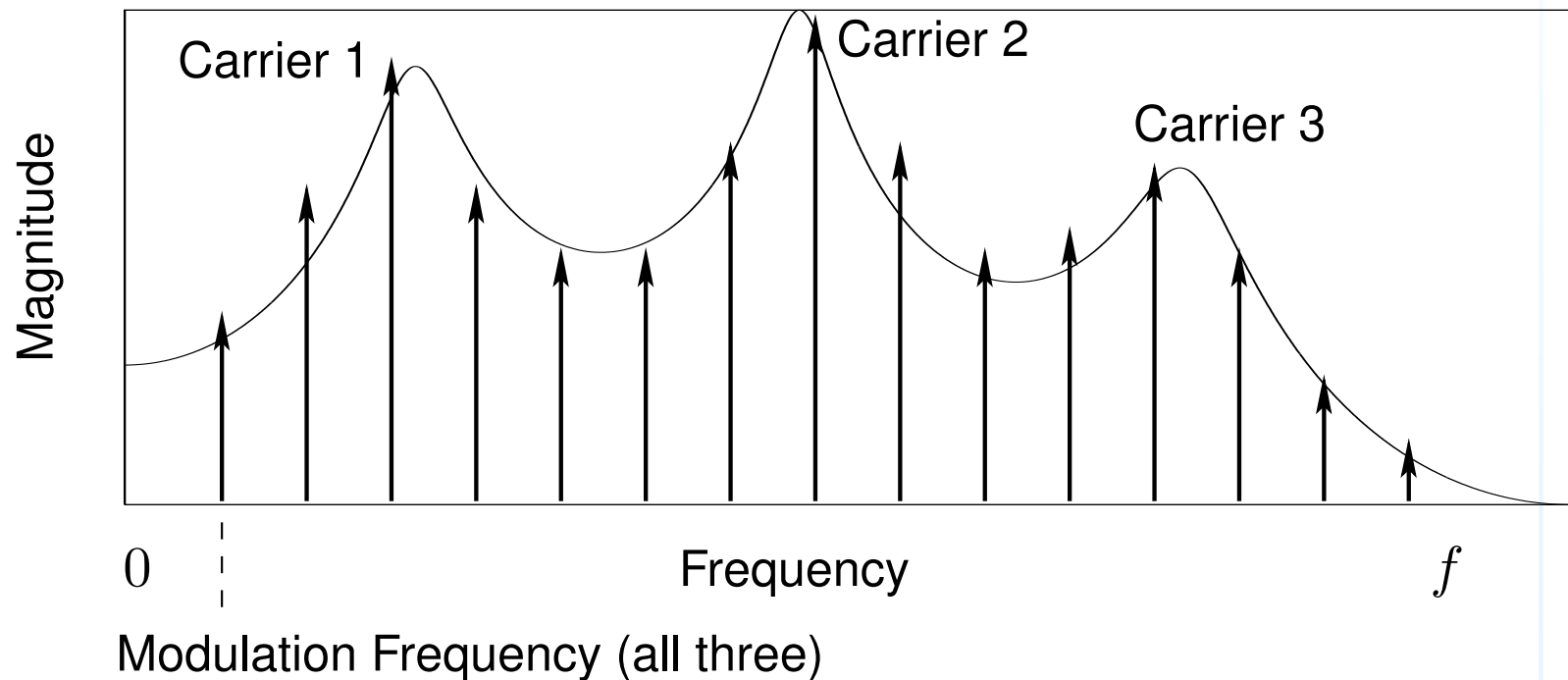
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FM voice synthesis can be viewed as *compressed modeling of spectral formants*





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Sampling Synthesis History

- 1979 - Fairlight Computer Music Instrument - 8-bit
 - First commercial sampler
 - Eight voices, 8 bits, 64 KB (4 sec) RAM, 16 kHz (mono)
 - Editing, looping, mixing
 - One could *draw* waveforms and additive-synthesis amplitude envelopes (for each harmonic) with a light pen
 - \$25,000–\$36,000!
- 1981 - E-mu Systems Emulator
 - First “affordable” sampler (\$10,000)
 - Eight voices, 128 K RAM, 8-bit, 80 lb.
- 1986 - Ensoniq Mirage
 - Breakthrough price-point (\$1695)
 - Eight voices, 144 K RAM, 8-bit



Modern Sampled Piano

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Example:¹

- 40 Gigabytes on ten DVDs (three sampled pianos)
- Every key sampled
- 4–10 “velocity layers”
- Separate recordings with soft pedal down
- Separate “release” recordings, for multiple striking velocities

¹Synthogy Ivory, \$349 (*Electronic Musician*, October 2006)



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Fundamental Problem with Sampling Synthesis

Piano timbre is determined by

- key number (1 byte)
- key velocity (2 bytes more than enough)
- pedal state (1 bit [or byte] per pedal)

Piano control is relatively low-dimensional:

- Less than six bytes of information per note played
- No continuous controls (typically)
- Ratio of total sampled data to one note of control data
 \approx one billion



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Now consider bowed strings

Control parameters:

- Left-hand finger position(s)
- Left-hand vibrato
- Bow velocity
- Bow force
- Bow position
- Bow angle
- Shoulder damping
- Instrument orientation
- Player motion (within a room)



Difficulty of sampling bowed strings

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- Bowed-string control is *infinite-dimensional* in principle
- Many *time-varying functions* — “gestures” (we counted more than 10)
- Complete sampling of bowed strings on the level of pianos has apparently never been done
- Rule-driven navigation of the *most useful* recorded playing regimes has worked well (*e.g.*, *Synful Orchestra*)
- *Model*-based approaches greatly reduce data requirements:
 - Spectral models (inspired by sound *perception*)
 - Physical models (model the sound *source*)



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Spectral Modeling Synthesis (Historical Summary)



Classic Vocoder Analysis & Resynthesis (Dudley 1939)

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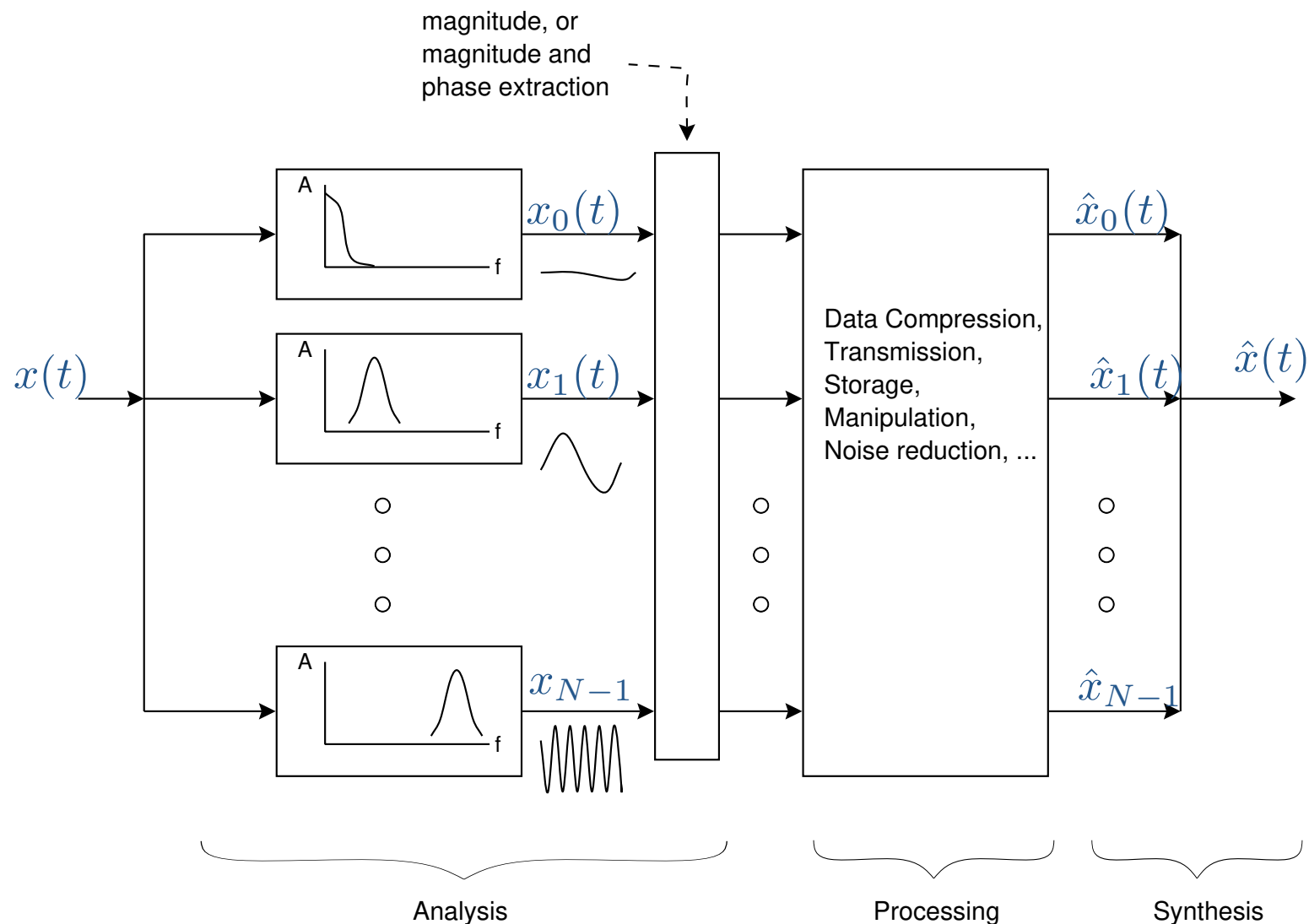
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Phase Vocoder Channel Model

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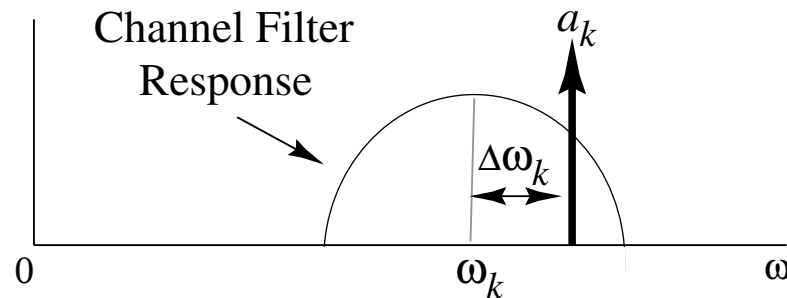
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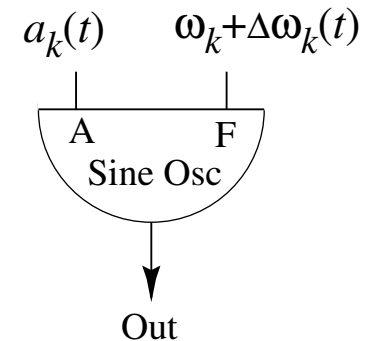
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Analysis Model



Synthesis Model



- Early “channel vocoder” implementations (hardware) only measured amplitude $a_k(t)$ (Dudley 1939)
- The “phase vocoder” (Flanagan and Golden 1966) added phase tracking in each channel
- Portnoff (1976) developed the FFT phase vocoder, which replaced the heterodyne comb in computer-music additive-synthesis analysis (James A. Moorer)
- Inverse FFT synthesis (Rodet and Depalle 1992) gave faster sinusoidal oscillator banks



Amplitude and Frequency Envelopes

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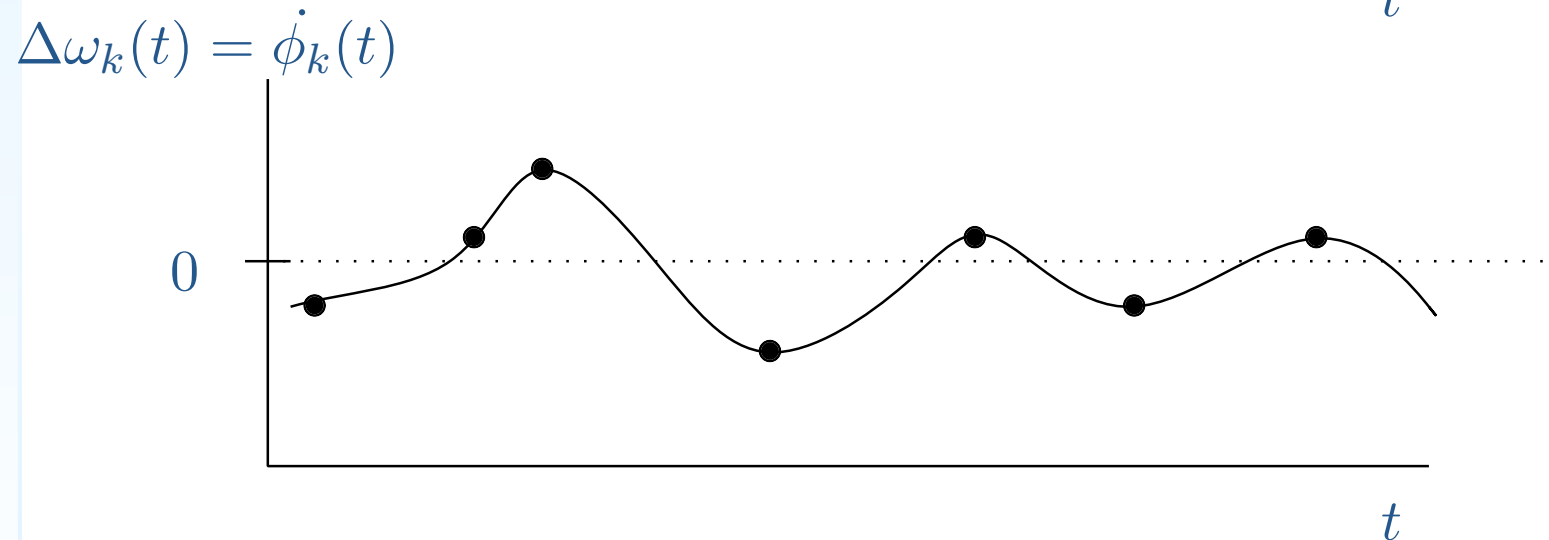
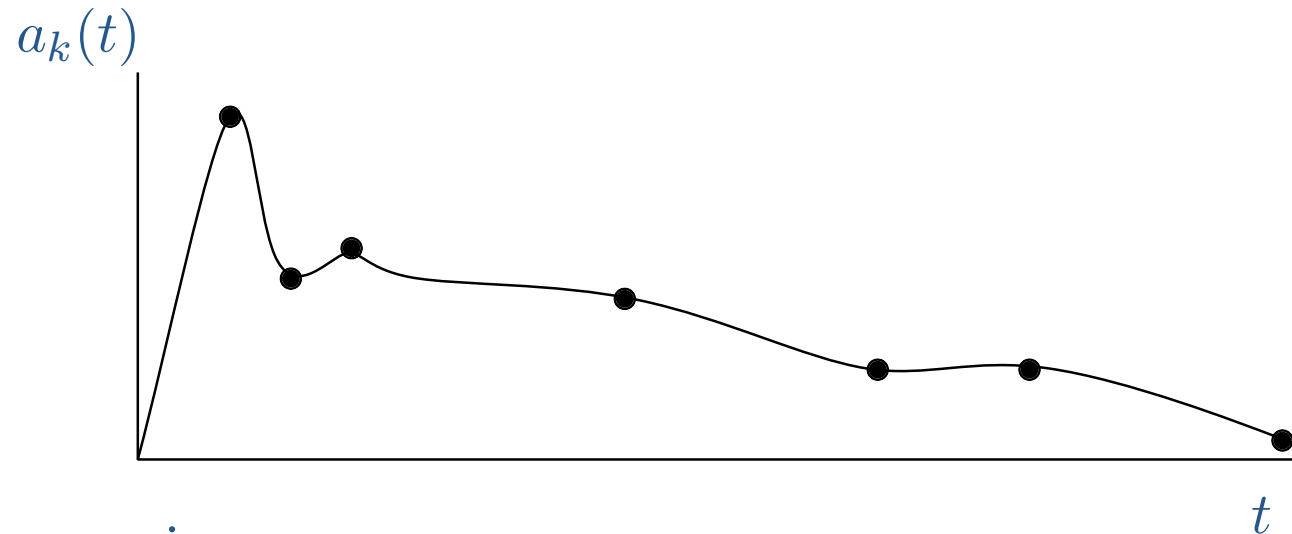
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Channel Vocoder Sound Examples

- Original
- 10 channels, sine carriers
- 10 channels, narrowband-noise carriers
- 26 channels, sine carriers
- 26 channels, narrowband-noise carriers
- 26 channels, narrowband-noise carriers, channels reversed
- **Phase Vocoder:** Identity system in absence of modifications
- The FFT Phase Vocoder next transitioned to the Short-Time Fourier Transform (STFT) (Allen and Rabiner 1977)



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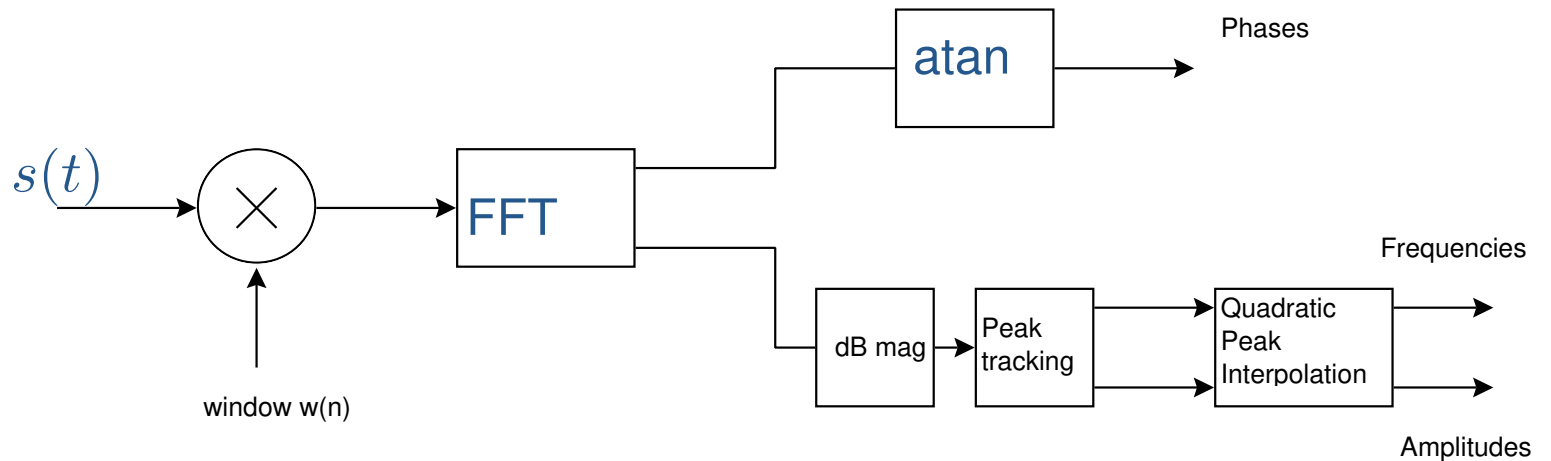
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Tracking Spectral Peaks in the Short-Time Fourier Transform



- STFT peak tracking at CCRMA: mid-1980s (PARSHL program)
- Motivated by vocoder analysis of piano tones
- Influences: STFT (Allen and Rabiner 1977), ADEC (1977), MAPLE (1979)
- Independently developed for speech coding by McAulay and Quatieri at Lincoln Labs



Example Spectral Trajectories

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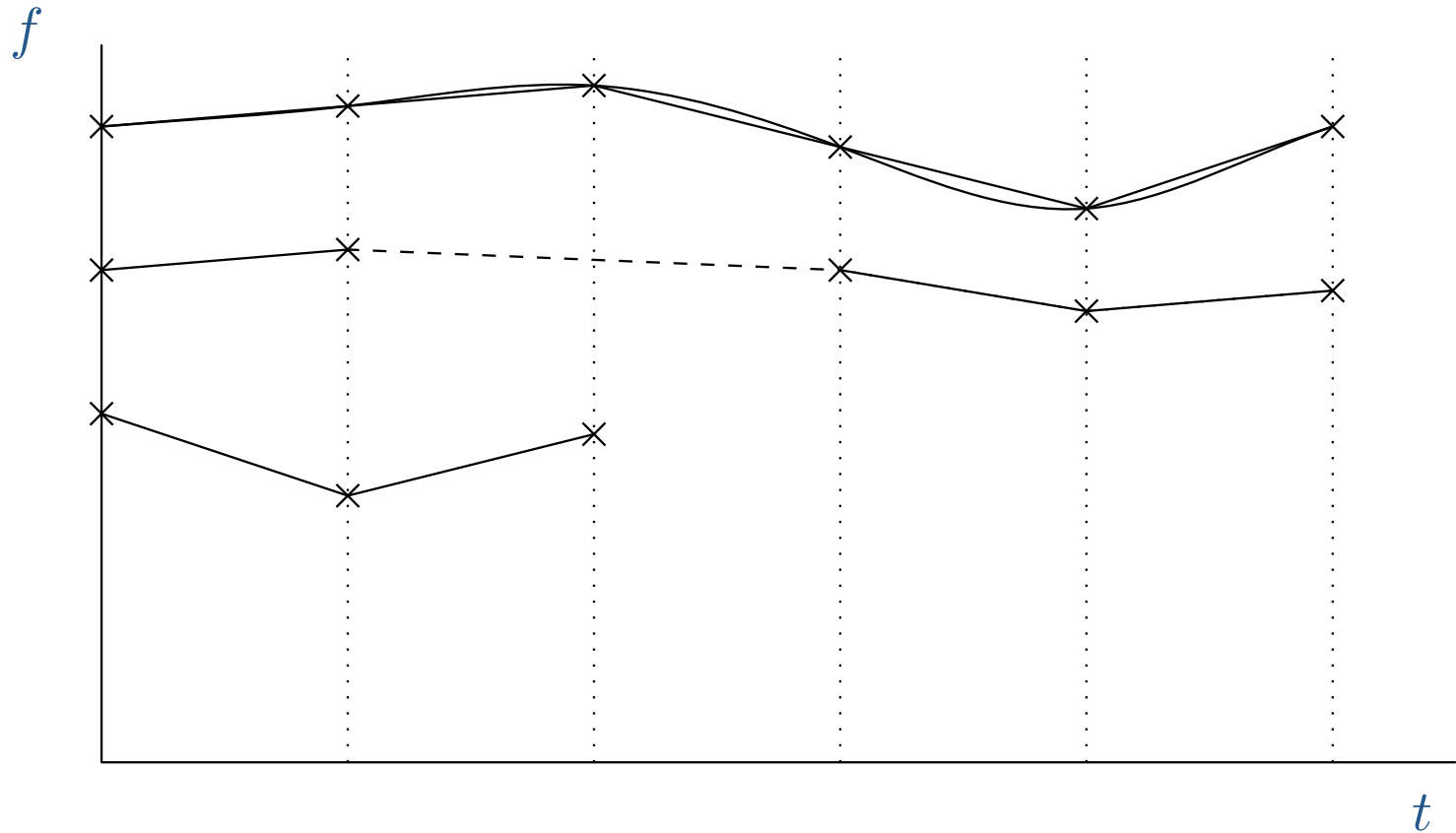
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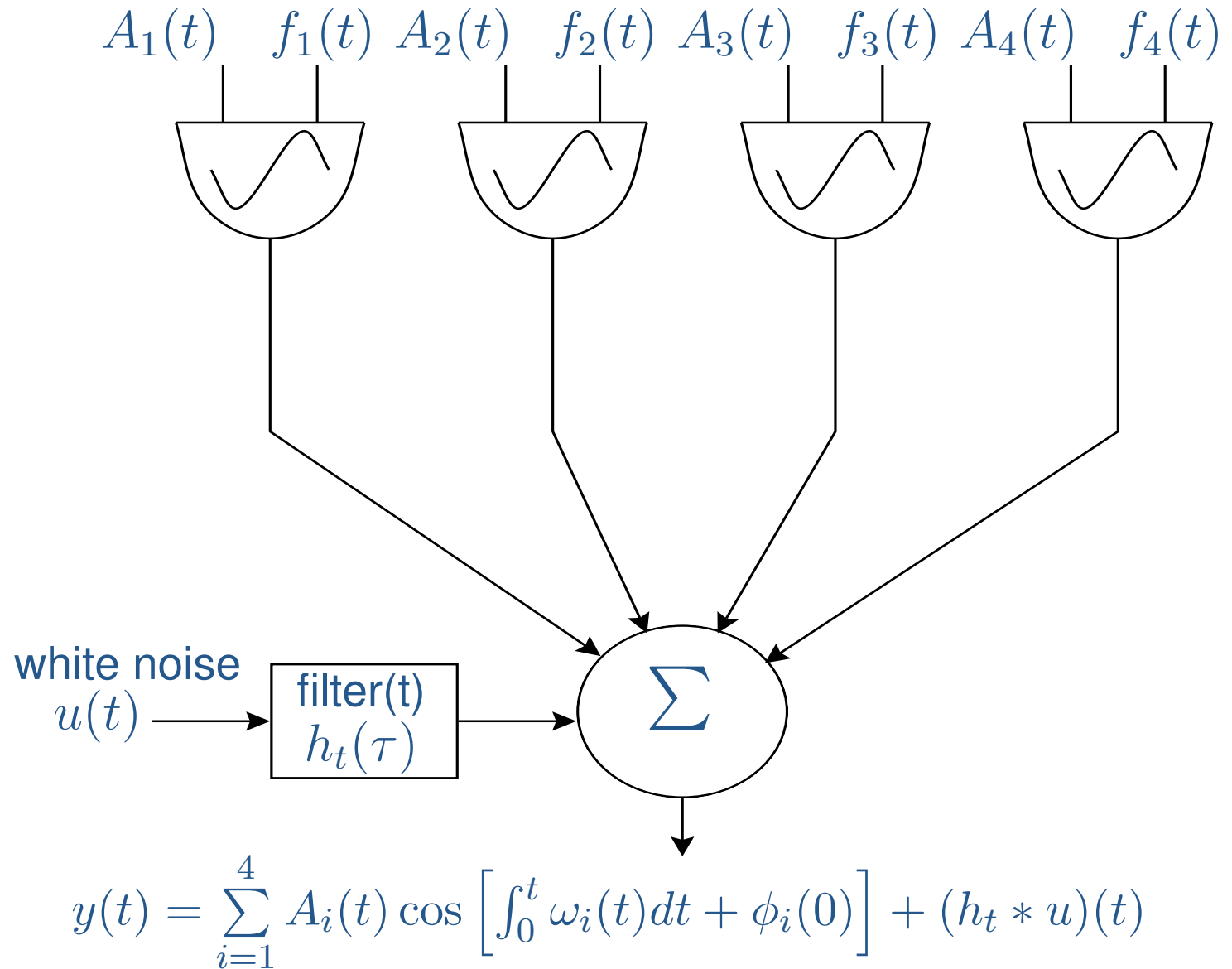
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Sines + Noise Synthesis (1989)





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Sines + Noise Sound Examples

Xavier Serra 1989 thesis demos (Sines + Noise signal modeling)

- Piano
 - Original
 - Sinusoids alone
 - Residual after sinusoids removed
 - Sines + noise model
- Voice
 - Original
 - Sinusoids
 - Residual
 - Synthesis



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Musical Effects with Sines+Noise Models (Serra 1989)

- Piano Effects
 - Pitch downshift one octave
 - Pitch flattened
 - Varying partial stretching
- Voice Effects
 - Frequency-scale by 0.6
 - Frequency-scale by 0.4 and stretch partials
 - Variable time-scaling, deterministic to stochastic



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Cross-Synthesis with Sines+Noise Models (Serra 1989)

- Voice “modulator”
- Creaking ship’s mast “carrier”
- Voice-modulated creaking mast
- Same with modified spectral envelopes



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Sines + Transients Sound Examples (Serra 1989)

In this technique, the sinusoidal sum is phase-matched at the cross-over point only (with no cross-fade).

- Marimba
 - Original
 - Sinusoidal model
 - Original attack, followed by sinusoidal model
- Piano
 - Original
 - Sinusoidal model
 - Original attack, followed by sinusoidal model



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Multiresolution Sines + Noise + Transients (Levine 1998)

Why Model Transients Separately?

- Sinusoids efficiently model spectral *peaks* over time
- Filtered noise efficiently models spectral *residual* vs. t
- Neither is good for *abrupt transients* in the waveform
- Phase-matched oscillators are expensive
- More efficient to switch to a *transient model* during transients
- Need sinusoidal *phase matching* at the switching times

Transient models:

- Original waveform slice (1988)
- Wavelet expansion (Ali 1996)
- MPEG-2 AAC (with short window) (Levine 1998)
- Frequency-domain LPC
(time-domain amplitude envelope) (Verma 2000)



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Early Digital Synthesis

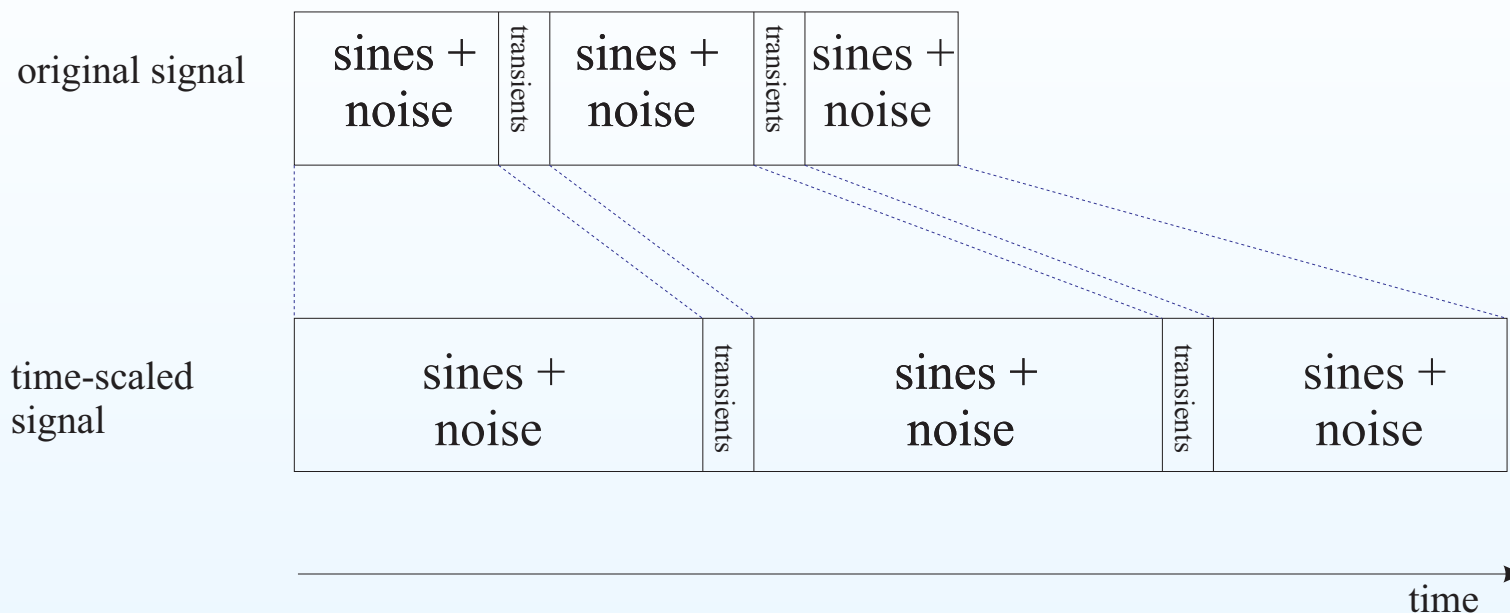
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Physical Modeling

Summary

Time Scale Modification of Sines + Noise + Transients Models



Time-Scale Modification (TSM) becomes *well defined*:

- Transients are *translated* in time
- Sinusoidal envelopes are *scaled* in time
- Noise-filter envelopes also *scaled* in time
- Dual of TSM is *frequency scaling*



Overview

Early Digital Synthesis

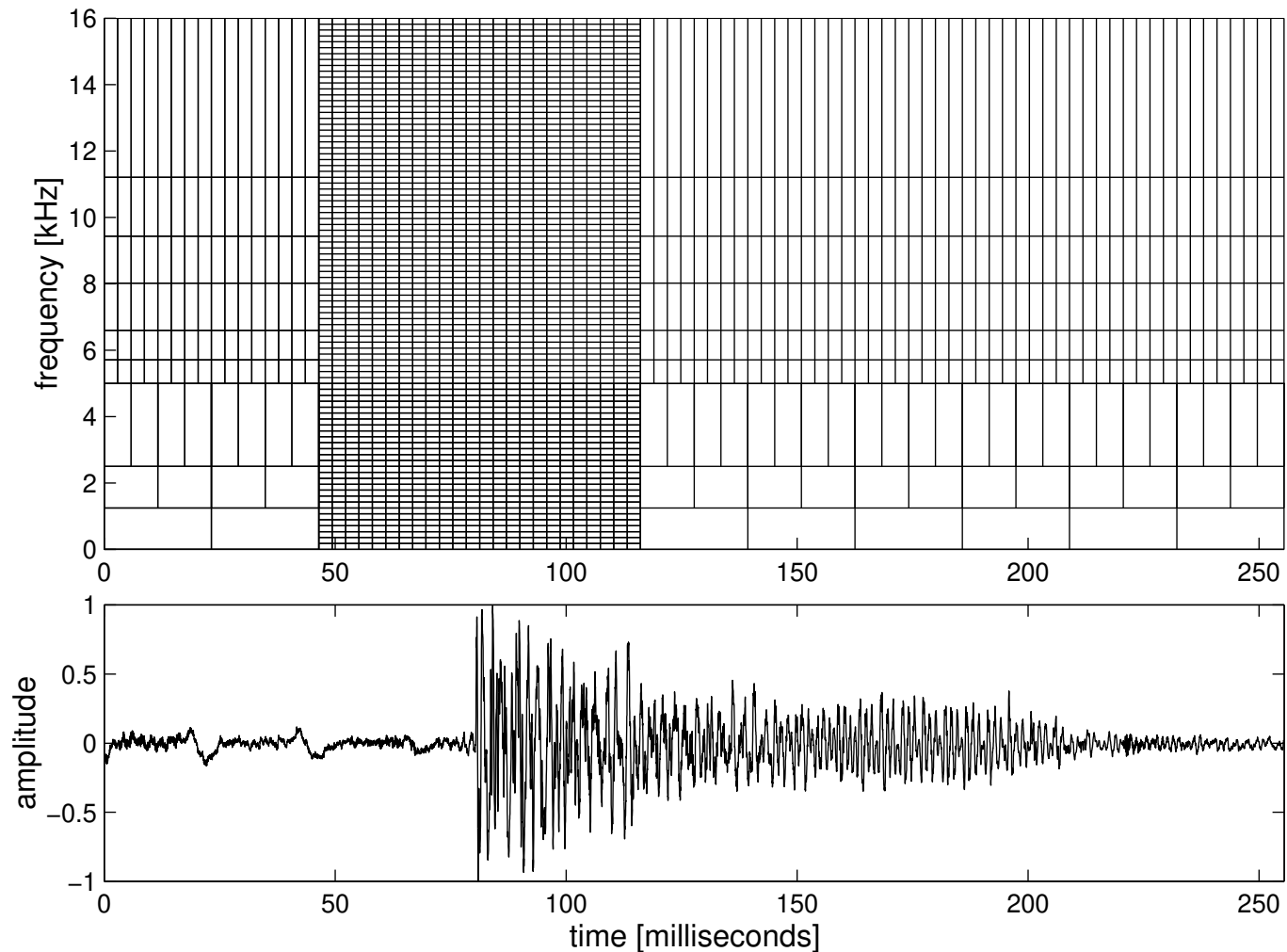
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Sines + Noise + Transients Time-Frequency Map



(Levine 1998)



Corresponding Analysis Windows

Overview

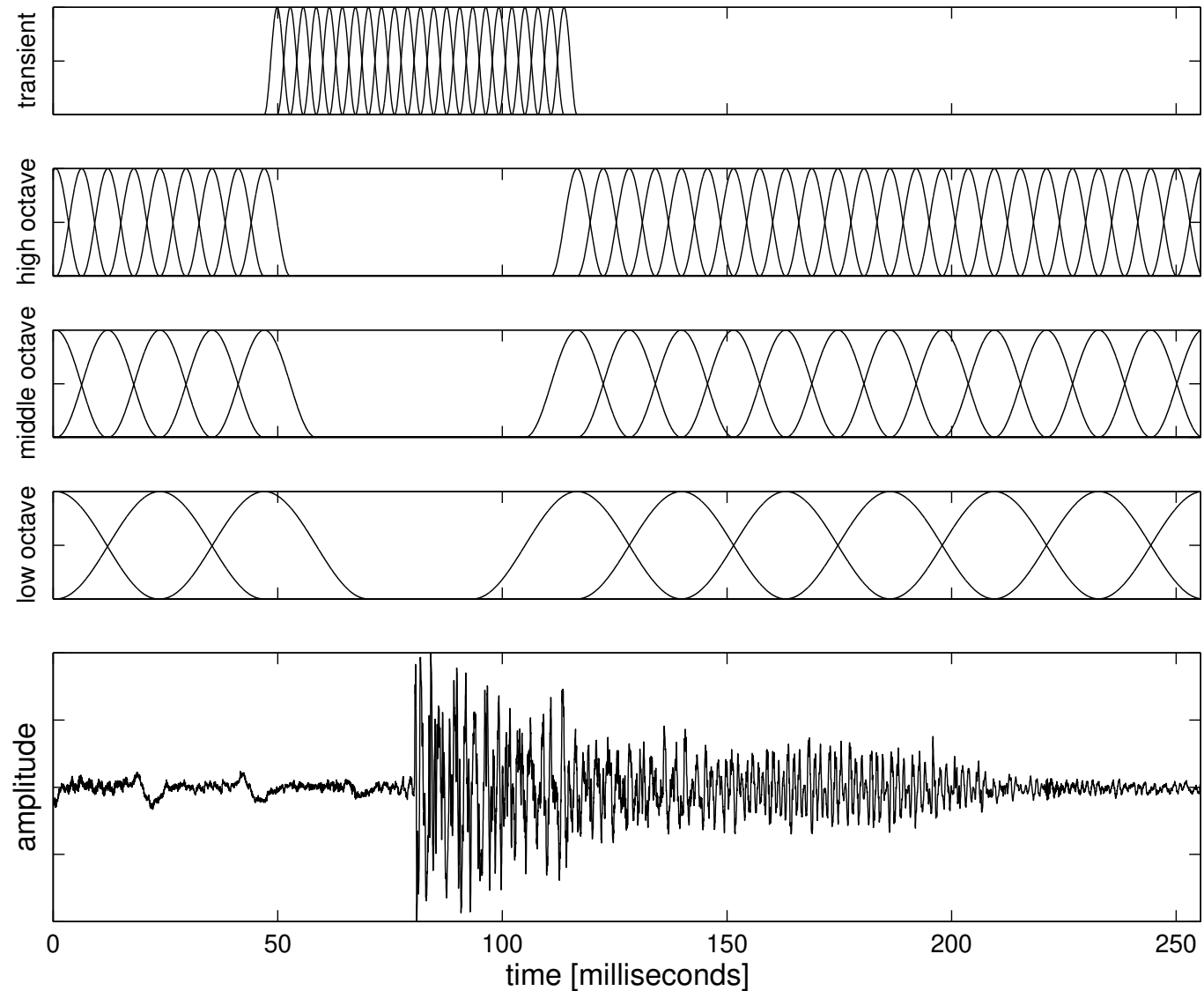
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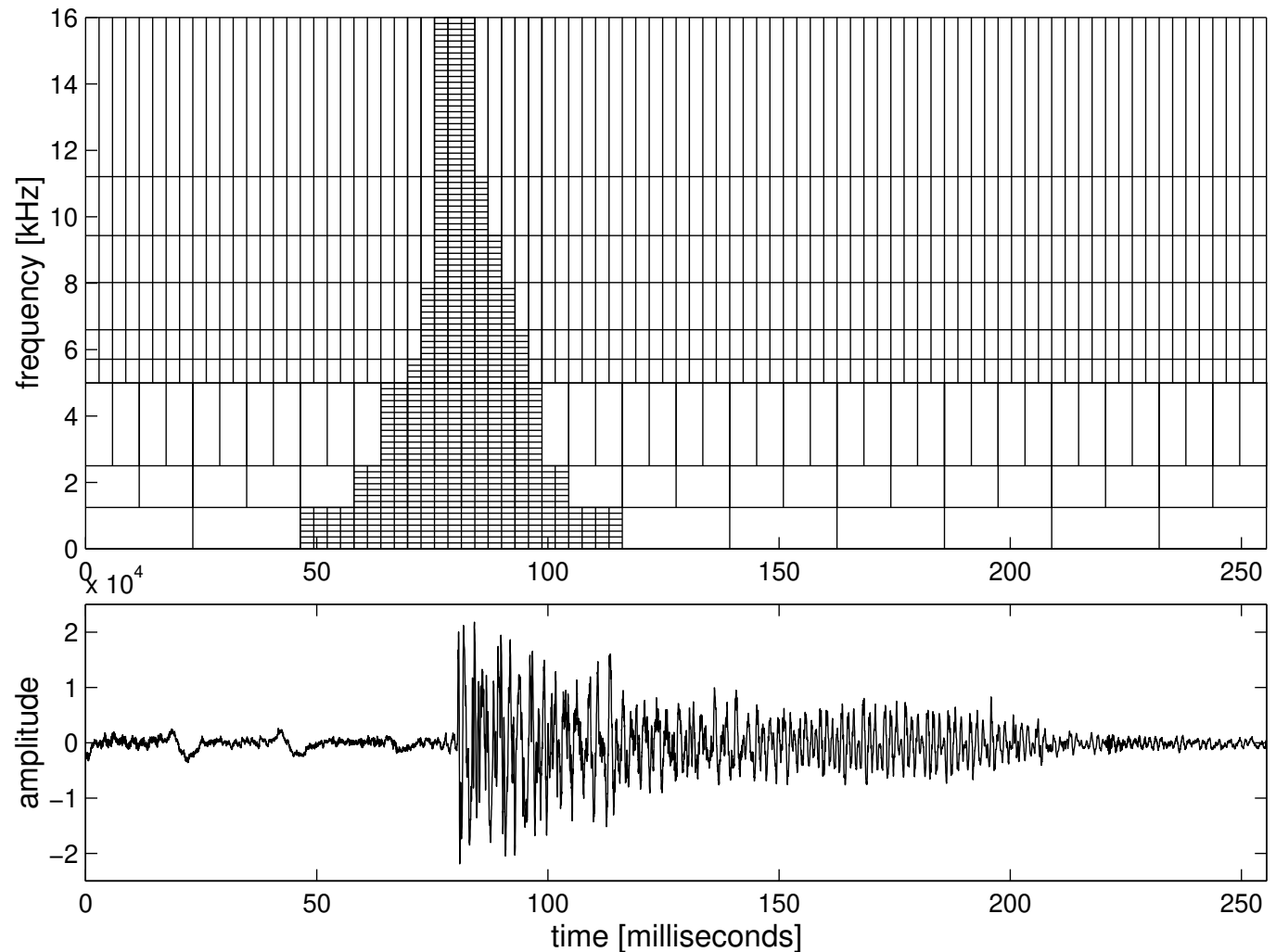
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Summary

Quasi-Constant-Q (Wavelet) Time-Frequency Map





Bark-Band Noise Modeling at High Frequencies (Levine 1998)

Overview

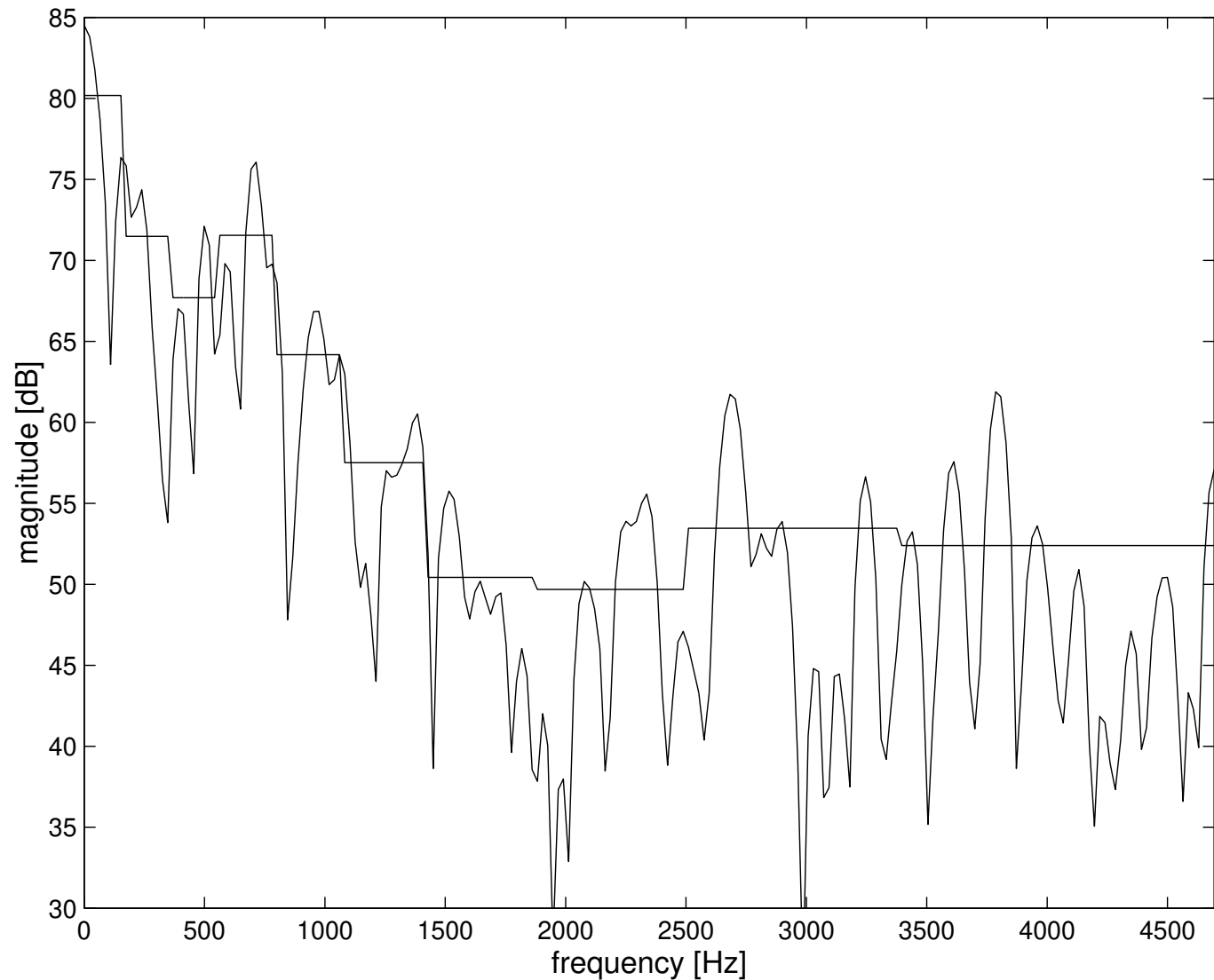
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Amplitude Envelope for One Noise Band

Overview

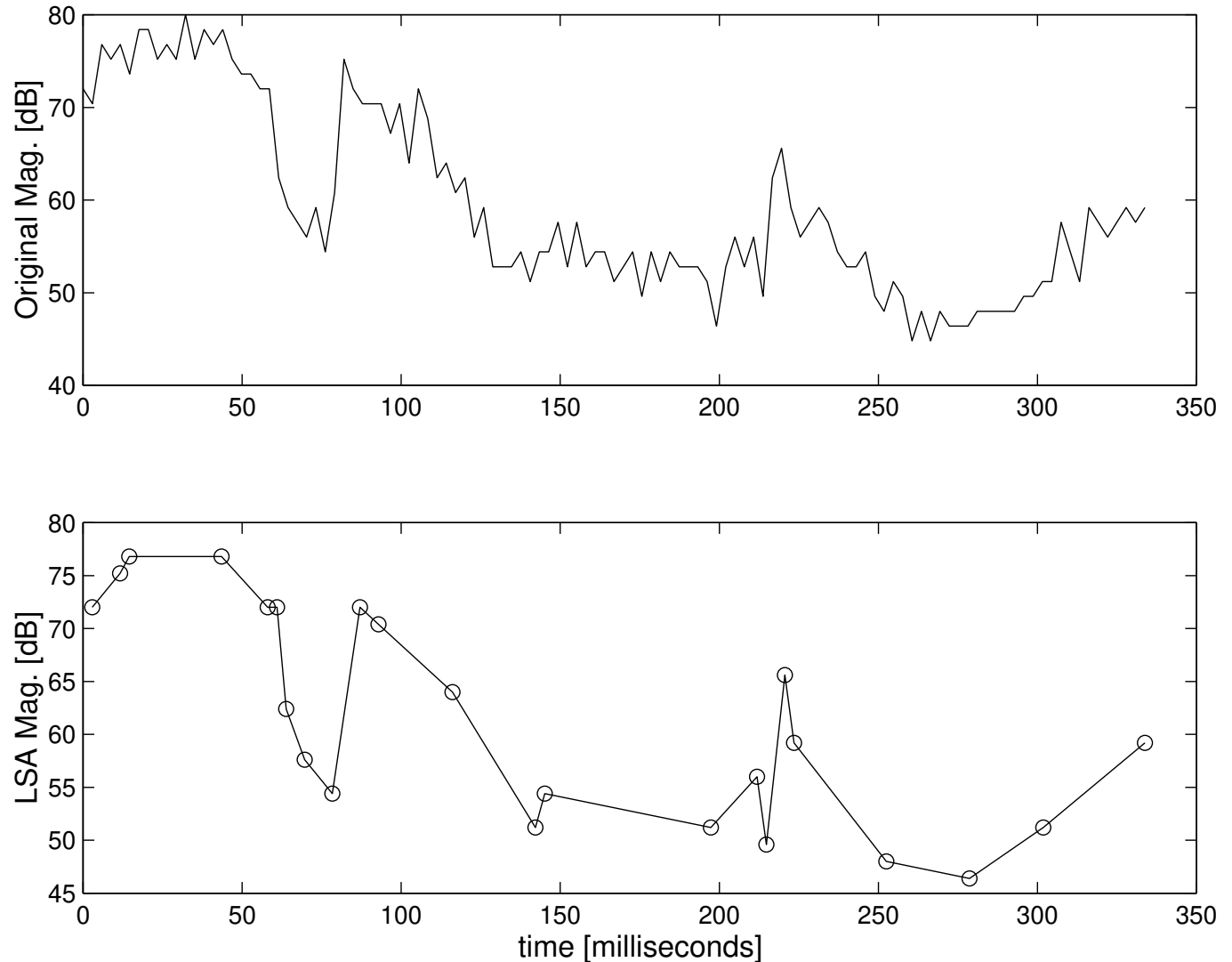
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For more information, see Scott Levine's thesis.²

²<http://ccrma.stanford.edu/scottl/thesis.html>



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Sines + Noise + Transients Sound Examples

Scott Levine Thesis Demos (Sines + Noise + Transients at 32 kbps)
(<http://ccrma.stanford.edu/~scottl/thesis.html>)

Mozart's Le Nozze di Figaro

- Original
- Compressed using MPEG-AAC at 32 kbps
- Compressed using sines+transients+noise at 32 kbps
- Multiresolution sinusoids alone
- Residual Bark-band noise
- Transform-coded transients (AAC)
- Bark-band noise above 5 kHz



Rock Example

Overview

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Scott Levine Thesis Demos (Sines + Noise + Transients at 32 kbps)
(<http://ccrma.stanford.edu/~scottl/thesis.html>)

“It Takes Two” by Rob Base & DJ E-Z Rock

- Original
- MPEG-AAC at 32 kbps
- Sines+transients+noise at 32 kbps
- Multiresolution sinusoids
- Residual Bark-band noise
- Transform-coded transients (AAC)
- Bark-band noise above 5 kHz



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Time Scale Modification using Sines + Noise + Transients

Scott Levine Thesis Demos (Sines + Noise + Transients at 32 kbps)
(<http://ccrma.stanford.edu/~scottl/thesis.html>)

Time-Scale Modification (pitch unchanged)

- S+N+T time-scale factors [2.0, 1.6, 1.2, 1.0, 0.8, 0.6, 0.5]

S+N+T Pitch Shifting (timing unchanged)

- Pitch-scale factors [0.89, 0.94, 1.00, 1.06, 1.12]

Spectral Modeling History Highlights

- Fourier's theory (1822)
- Teleharmonium (1906)
- Hammond organ (1930s)
- Channel Vocoder (1939)
- Phase Vocoder (1966)
- "Additive Synthesis" (1969)
- FFT Phase Vocoder (1976)
- Sinusoidal Modeling (1977,1979,1985)
- Sines+Noise (1989)
- Sines+Transients (1989)
- Sines+Noise+Transients (1998)

Perceptual audio coding:

- Princen-Bradley filterbank (1986)
- K. Brandenburg thesis (1989)
- *Auditory masking* usage
- Dolby AC2
- Musicam
- ASPEC
- MPEG-I,II,IV
(incl. S+N+T "parametric sounds")



Future Prospects

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Physical Modeling

Summary

Observations:

- Sinusoidal modeling of sound is “Unreasonably Effective”
- Basic “auditory masking” discards $\approx 90\%$ information
- Interesting neuroscience observation:

“... most neurons in the primary auditory cortex A1 are silent most of the time ...”

(from “Sparse Time-Frequency Representations”, Gardner and Magnesco, PNAS:103(16), April 2006)

- What is a true and correct “psychospectral model” for sound?
 - The cochlea of the ear is a real-time spectrum analyzer
 - How is the “ear’s spectrogram” represented at higher levels?



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Physical Modeling Synthesis (Historical Summary)



Kelly-Lochbaum Vocal Tract Model

Overview

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Spectral Modeling

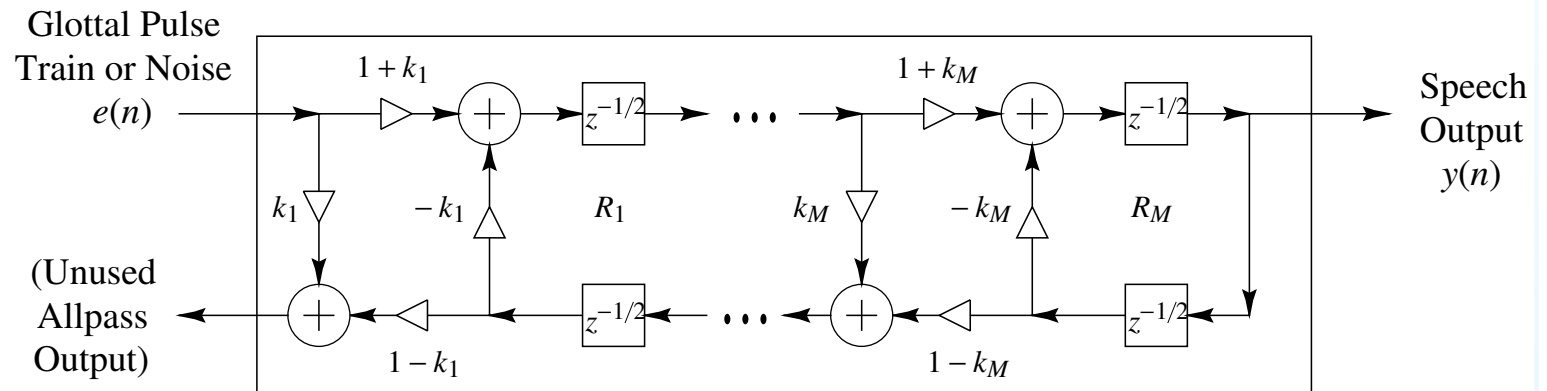
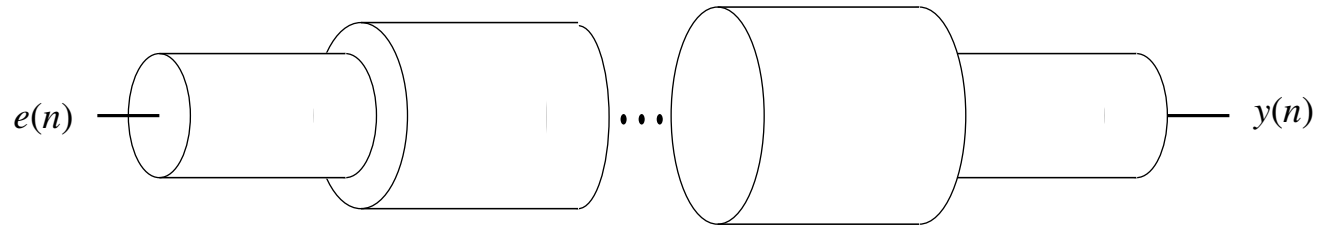
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- Phy Audio Coding?

Summary

Julius Smith



Kelly-Lochbaum Vocal Tract Model (Pieewise Cylindrical)

John L. Kelly and Carol Lochbaum (1962)





Overview

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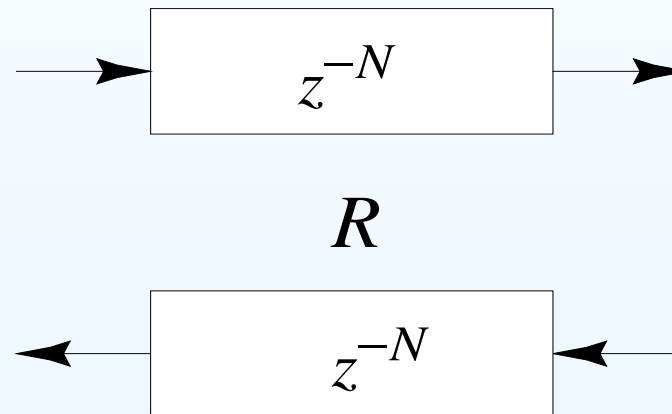
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Summary

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Digital Waveguide Models (1985)

*Lossless digital waveguide \triangleq bidirectional delay line
at some wave impedance R*



Useful for efficient models of

- strings
- bores
- plane waves
- conical waves





Signal Scattering

Overview

Early Digital Synthesis

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Physical Modeling

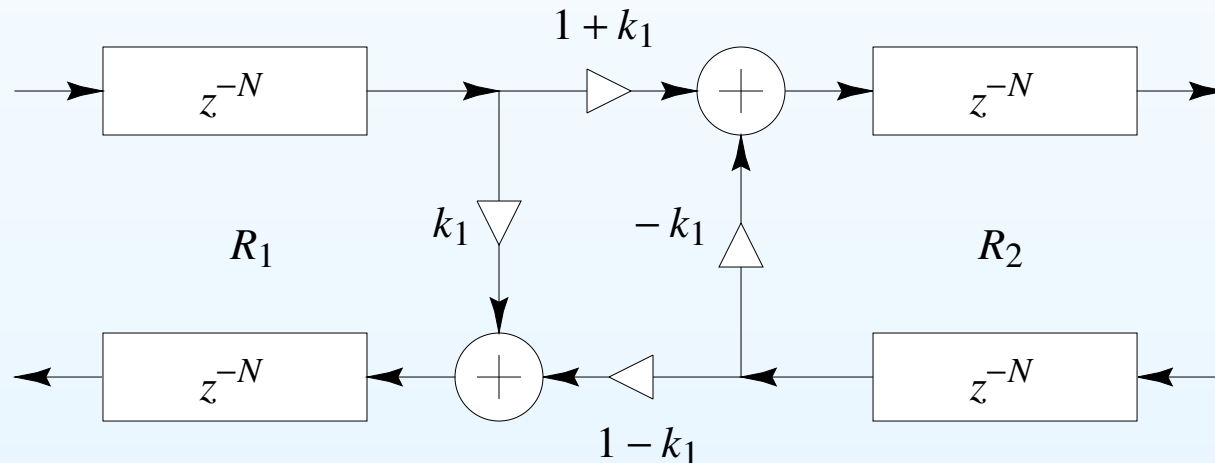
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Summary

Julius Smith

Signal *scattering* is caused by a *change* in wave impedance R :

$$k_1 = \frac{R_2 - R_1}{R_2 + R_1}$$



If the wave impedance changes *every spatial sample*, the Kelly-Lochbaum vocal-tract model results.





Ideal Plucked String (Displacement Waves)

Overview

Early Digital Synthesis

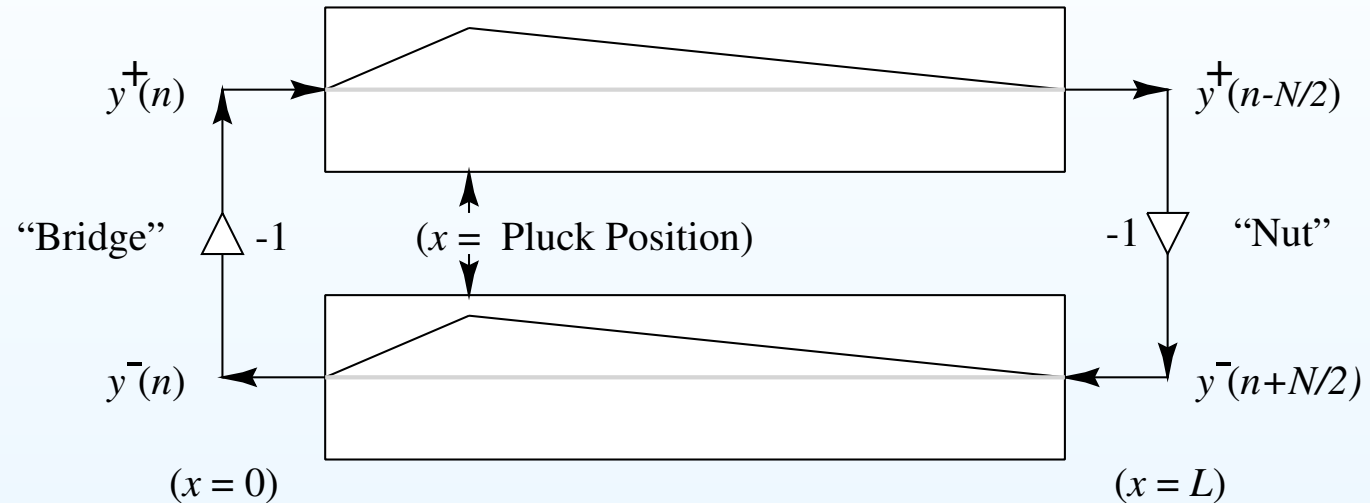
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Summary

Julius Smith



- Load each delay line with *half* of initial string displacement
- Sum of upper and lower delay lines = string displacement





Ideal Struck String (Velocity Waves)

Overview

Early Digital Synthesis

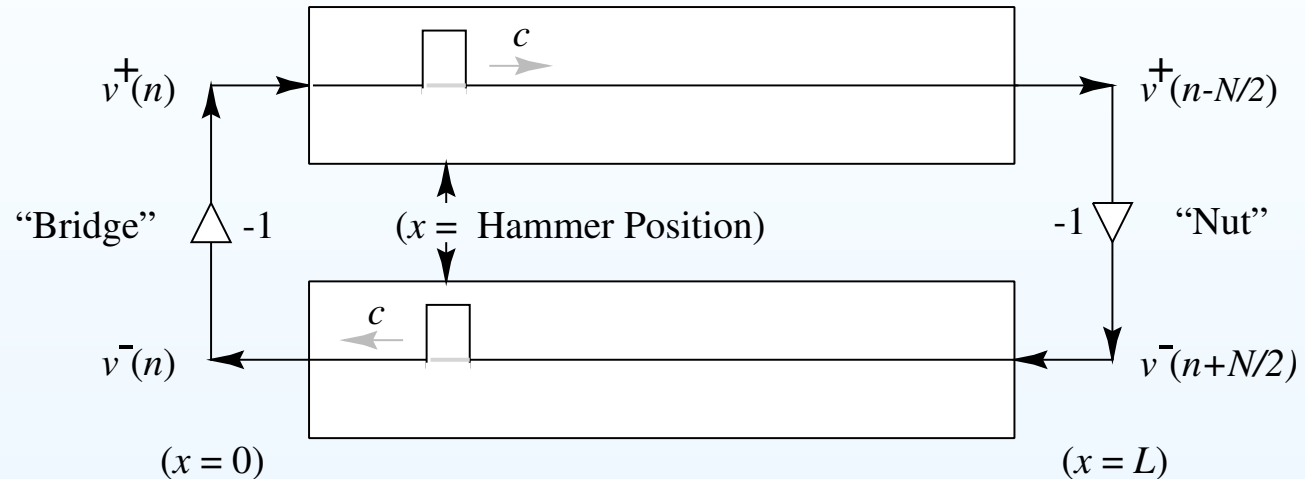
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Summary

Julius Smith



Hammer strike = *momentum transfer* = velocity step:

$$m_h v_h(0-) = (m_h + m_s) v_s(0+)$$





Karplus-Strong (KS) Algorithm (1983)

Overview

Early Digital Synthesis

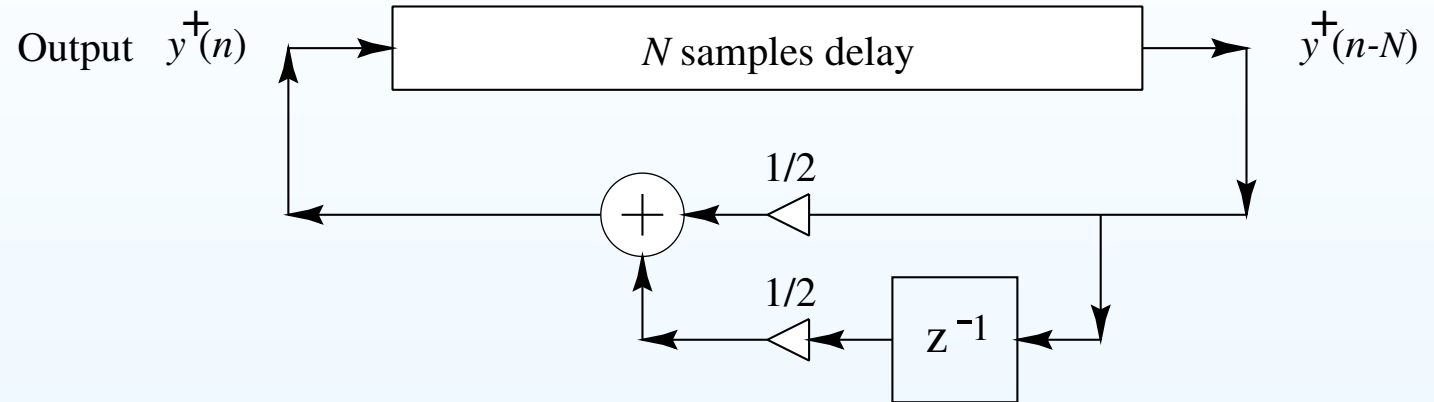
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Summary

Julius Smith



- Discovered (1978) as “self-modifying wavetable synthesis”
- Wavetable is preferably initialized with random numbers





Karplus-Strong Sound Examples

Overview

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Summary

Julius Smith

- “Vintage” 8-bit sound examples:
 - Original Plucked String: (WAV) (MP3)
 - Drum: (WAV) (MP3)
 - Stretched Drum: (WAV) (MP3)





EKS Algorithm (Jaffe-Smith 1983)

Overview

Early Digital Synthesis

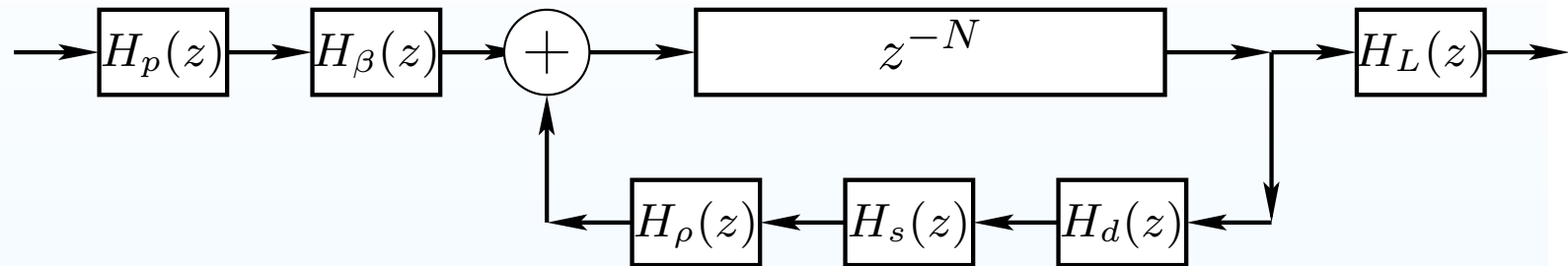
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Summary

Julius Smith



N = pitch period ($2 \times$ string length) in samples

$H_p(z) = \frac{1-p}{1-pz^{-1}}$ = pick-direction lowpass filter

$H_\beta(z) = 1 - z^{-\beta N}$ = pick-position comb filter, $\beta \in (0, 1)$

$H_d(z)$ = string-damping filter (one/two poles/zeros typical)

$H_s(z)$ = string-stiffness allpass filter (several poles and zeros)

$H_\rho(z) = \frac{\rho(N) - z^{-1}}{1 - \rho(N)z^{-1}}$ = first-order string-tuning allpass filter

$H_L(z) = \frac{1 - R_L}{1 - R_L z^{-1}}$ = dynamic-level lowpass filter





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Summary

Julius Smith

STK EKS Sound Examples

- Synthesis Tool Kit (STK) by Perry Cook, Gary Scavone, and others — distributed by CCRMA:
Google search: *STK ToolKit*

STK Plucked String: (WAV) (MP3)

- Plucked String 1: (WAV) (MP3)
- Plucked String 2: (WAV) (MP3)
- Plucked String 3: (WAV) (MP3)





EKS Sound Example (1988)

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Summary

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Bach A-Minor Concerto—Orchestra Part: (WAV) (MP3)

- Executed in real time on one Motorola DSP56001 (20 MHz clock, 128K SRAM)
- Developed for the NeXT Computer introduction at Davies Symphony Hall, San Francisco, 1988
- Solo violin part was played live by Dan Kobialka of the San Francisco Symphony





Overview

Early Digital Synthesis

Spectral Modeling

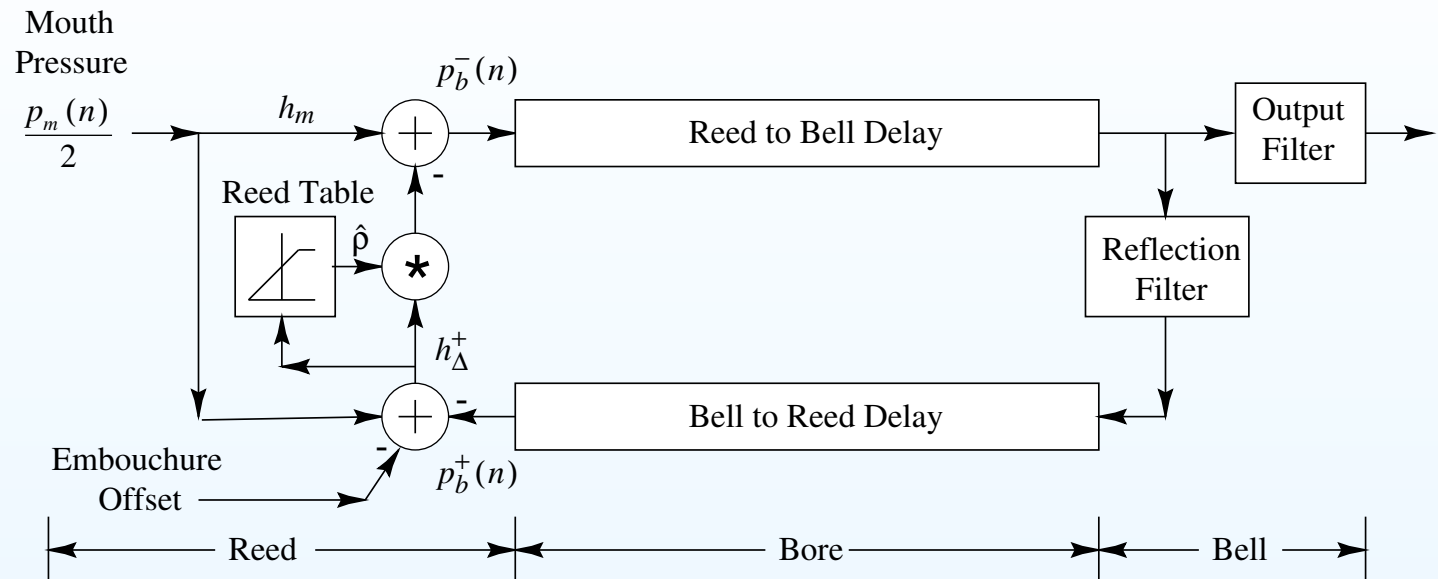
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Summary

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Digital Waveguide Single Reed, Cylindrical Bore Model (1986)



Digital waveguide clarinet

- Control variable = mouth half-pressure
- Total reed cost = two subtractions, one multiply, and one table lookup per sample





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Julius Smith

Digital Waveguide Wind Instrument Sound Examples

- STK Clarinet: (WAV) (MP3)
Google search: *STK clarinet*
 - Synthesis Tool Kit (STK) by Perry Cook, Gary Scavone, and others — distributed by CCRMA:
Google search: *STK ToolKit*
- Staccato Systems Slide Flute
(based on STK flute, ca. 1995): (WAV) (MP3)
- Yamaha VL1 “Virtual Lead” synthesizer demos (1994):
 - Shakuhachi: (WAV) (MP3)
 - Oboe and Bassoon: (WAV) (MP3)
 - Tenor Saxophone: (WAV) (MP3)





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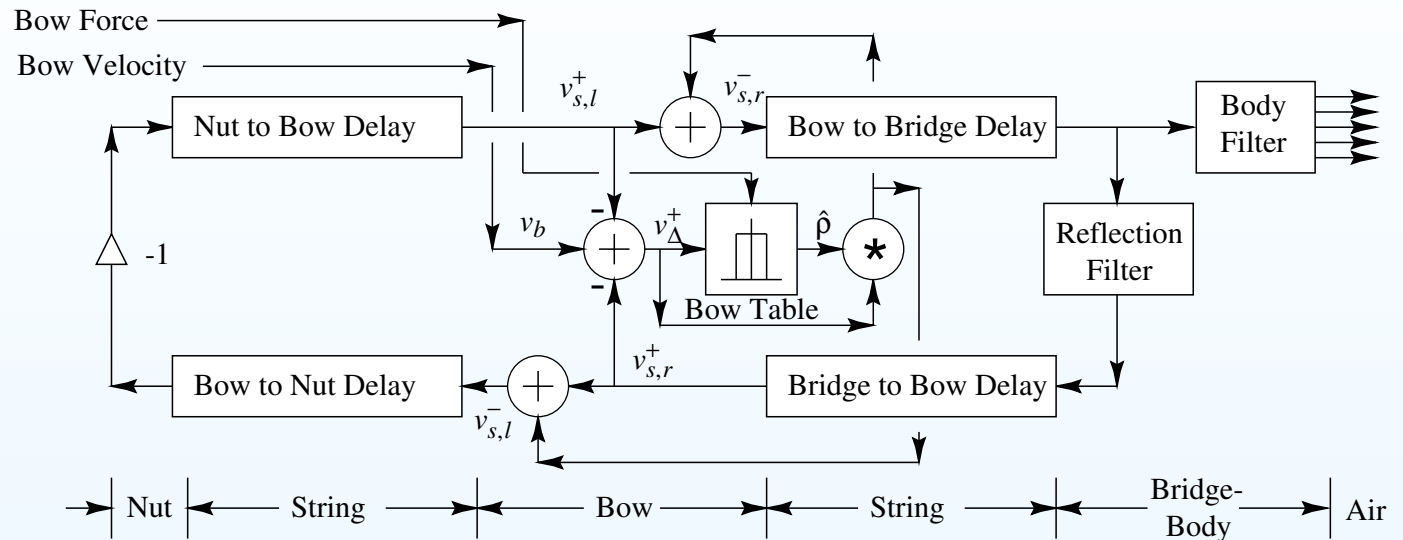
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Julius Smith

Digital Waveguide Bowed Strings (1986)



- Reflection filter summarizes all losses per period (due to bridge, bow, finger, etc.)
- Bow-string junction = *memoryless* lookup table (or segmented polynomial)





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“Electric Cello” Sound Examples (Peder Larson)

- Staccato Notes: (WAV) (MP3)
(short strokes of high bow pressure, as from a bouncing bow)
- Bach’s First Suite for Unaccompanied Cello: (WAV) (MP3)





Soft Clipper

Overview

Early Digital Synthesis

Spectral Modeling

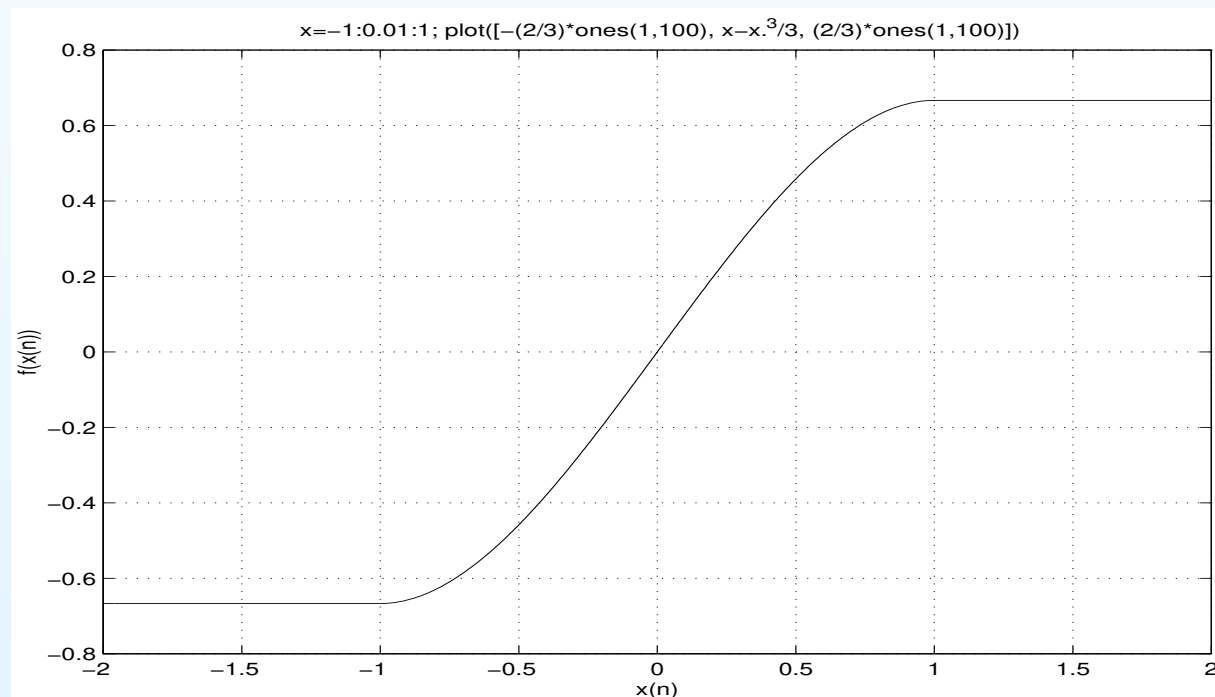
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Julius Smith

$$f(x) = \begin{cases} -\frac{2}{3}, & x \leq -1 \\ x - \frac{x^3}{3}, & -1 \leq x \leq 1 \\ \frac{2}{3}, & x \geq 1 \end{cases}$$





Amplifier Distortion + Amplifier Feedback

Sullivan 1990

Overview

Early Digital Synthesis

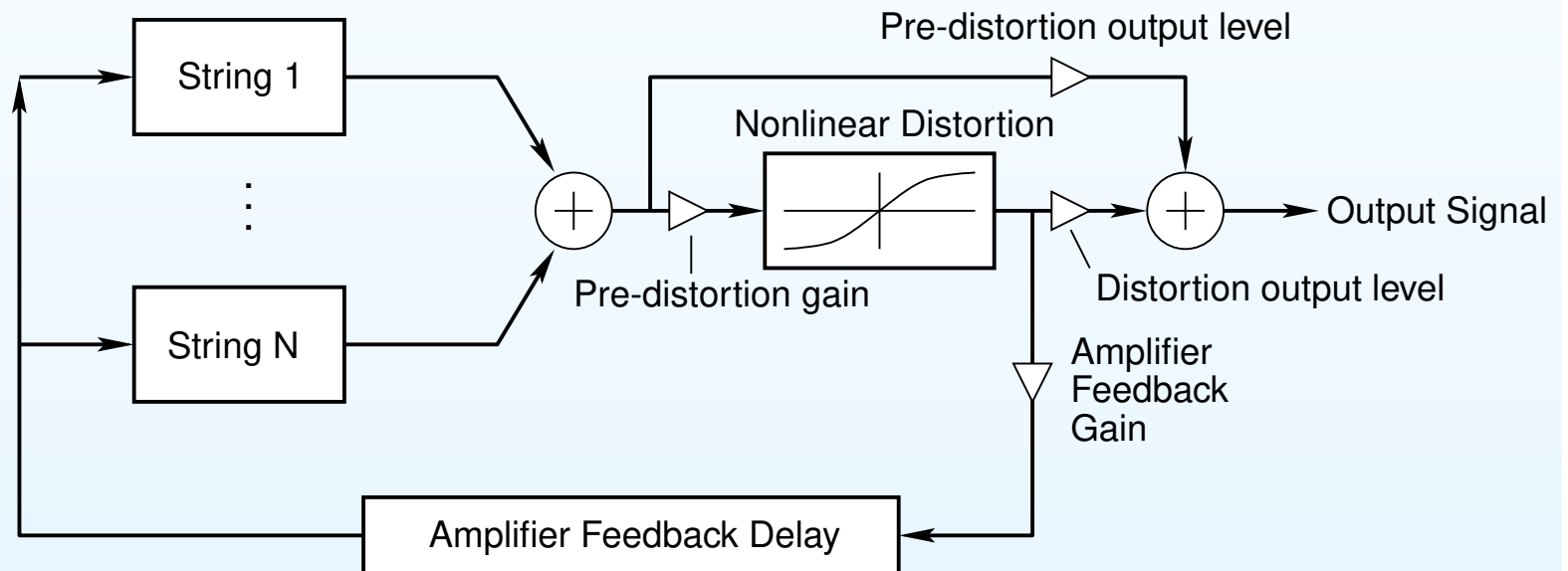
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Julius Smith



Distortion output signal often further filtered by an *amplifier cabinet filter*, representing speaker cabinet, driver responses, etc.





Distortion Guitar Sound Examples

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(Stanford Sondius Project, ca. 1995)

- Distortion Guitar: (WAV) (MP3)
- Amplifier Feedback 1: (WAV) (MP3)
- Amplifier Feedback 2: (WAV) (MP3)

Summary

Julius Smith





Overview

Early Digital Synthesis

Spectral Modeling

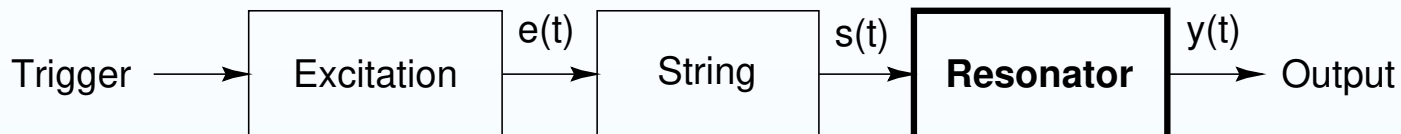
Physical Modeling

- KL Music
- Digital Waveguide
- Signal Scattering
- Plucked String
- Struck String
- Karplus Strong
- EKS Algorithm
- Clarinet
- Wind Examples
- Bowed Strings
- Distortion Guitar
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- Sound Examples
- Linearized Violin
- Commuted Piano
- Pulse Synthesis
- Complete Piano
- Sound Examples
- Phy Audio Coding
- Phy Audio Coding?

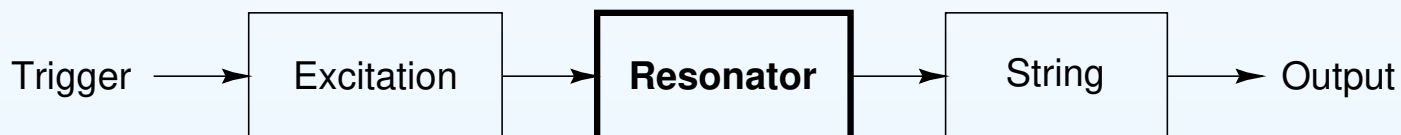
Summary

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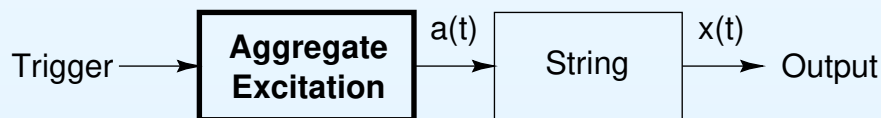
Commutated Synthesis of Acoustic Strings (1993)



Schematic diagram of a stringed musical instrument.



Equivalent diagram in the linear, time-invariant case.



Use of an aggregate excitation given by the convolution of original excitation with the resonator impulse response.





Commuted Components

Overview

Early Digital Synthesis

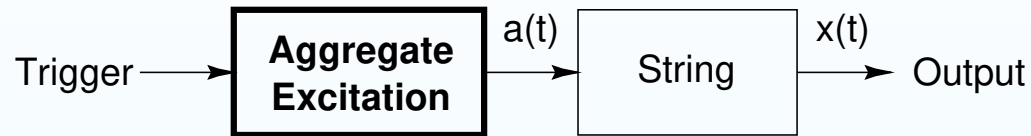
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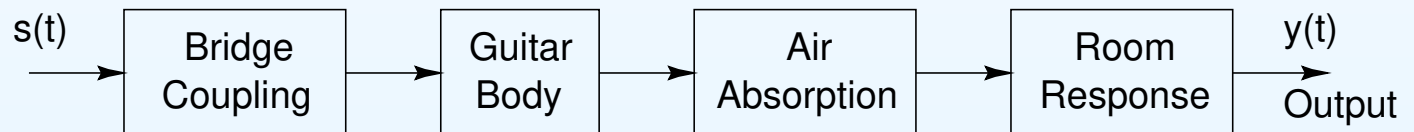
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“Plucked Resonator” driving a String.



Possible components of a guitar resonator.





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Sound Examples

Electric Guitar (Pick-Ups and/or Body-Model Added) (Stanford Sondius Project → Staccato Systems, Inc. → ADI, ca. 1995)

- Example 1: (WAV) (MP3)
- Example 2: (WAV) (MP3)
- Example 3: (WAV) (MP3)
- Virtual “wah-wah pedal”: (WAV) (MP3)

STK Mandolin

- STK Mandolin 1: (WAV) (MP3)
- STK Mandolin 2: (WAV) (MP3)





Sound Examples

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More Recent Acoustic Guitar

- Bach Prelude in E Major: (WAV) (MP3)
- soundexamplewavBach silenceLoure in E Major: (WAV) (MP3)

Virtual performance by Dr. Mikael Laurson, Sibelius Institute

Virtual guitar by Helsinki Univ. of Tech., Acoustics Lab³

³<http://www.acoustics.hut.fi/>





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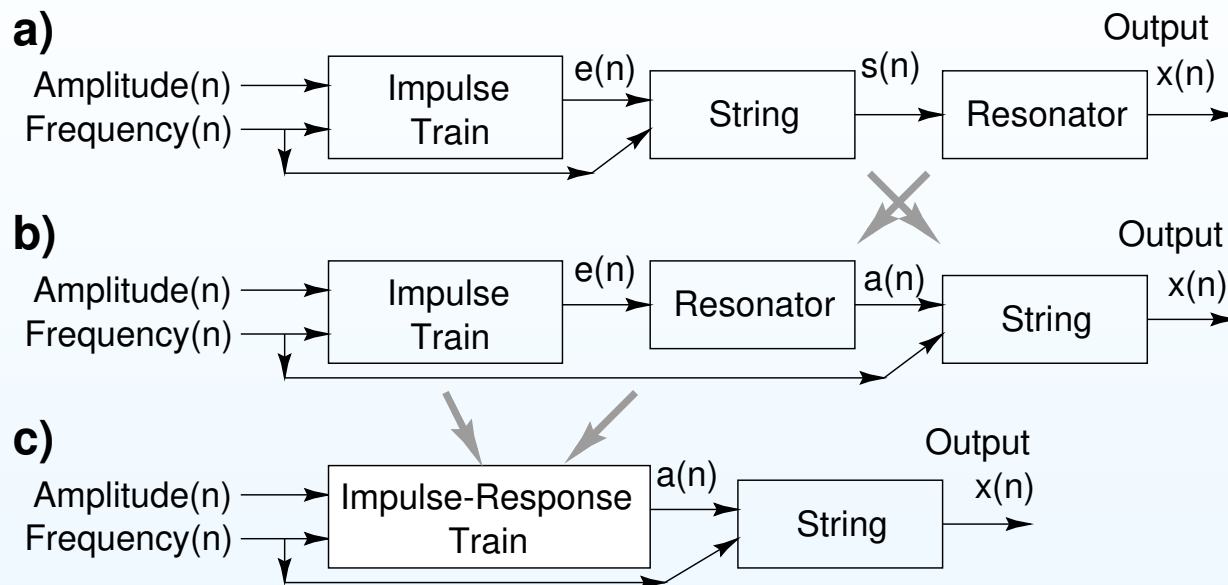
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Summary

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Commuted Synthesis of Linearized Violin



- Assumes *ideal Helmholtz motion* of string
- Sound Examples (Stanford Sondius project, ca. 1995):
 - Bass: (WAV) (MP3)
 - Cello: (WAV) (MP3)
 - Viola 1: (WAV) (MP3)
 - Viola 2: (WAV) (MP3)
 - Violin 1: (WAV) (MP3)
 - Violin 2: (WAV) (MP3)
 - Ensemble: (WAV) (MP3)





Commuted Piano Synthesis (1995)

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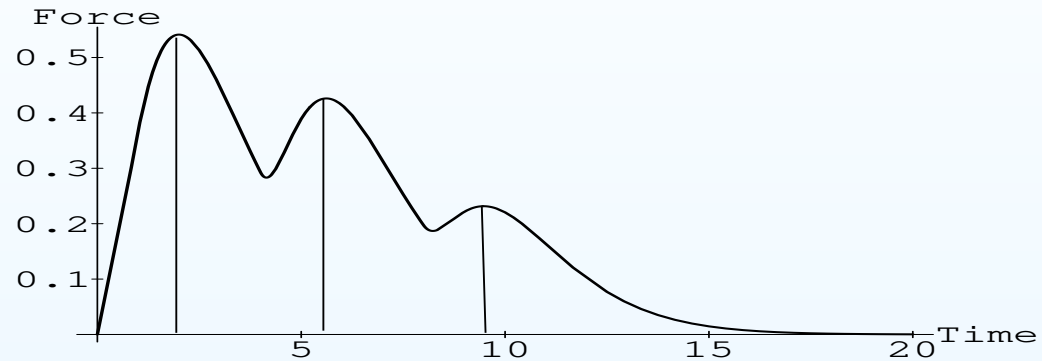
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Summary

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Hammer-string interaction pulses (force):





Synthesis of Hammer-String Interaction Pulse

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Early Digital Synthesis

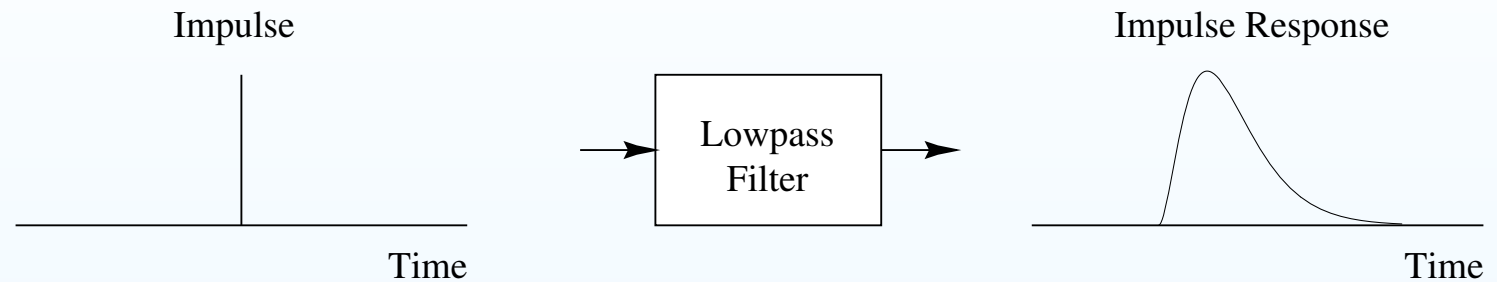
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- Faster collisions correspond to *narrower* pulses (*nonlinear filter*)
- For a *given velocity*, filter is linear time-invariant
- Piano is “linearized” for each hammer velocity





Overview

Early Digital Synthesis

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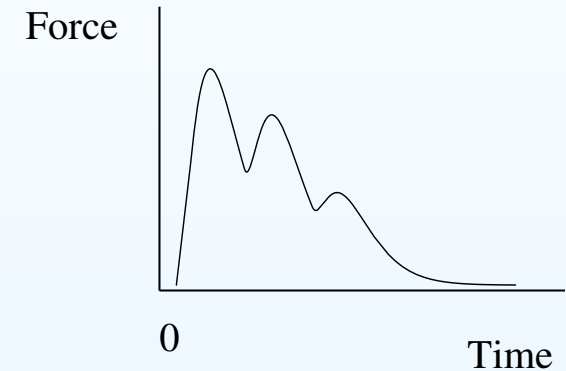
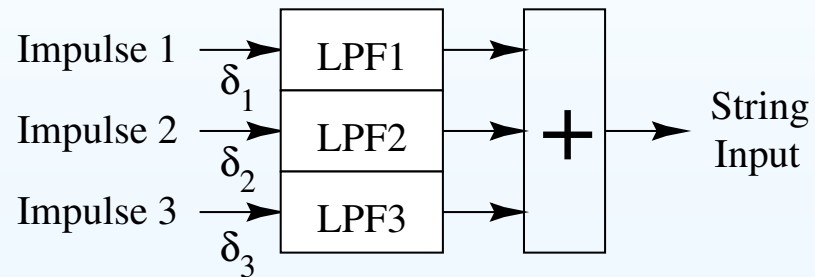
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Summary

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Multiple Hammer-String Interaction Pulses

Superimpose several individual pulses:





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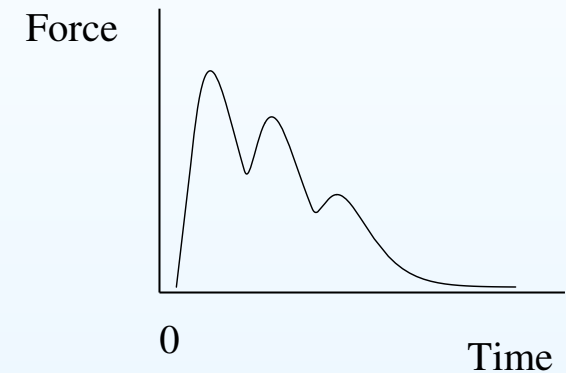
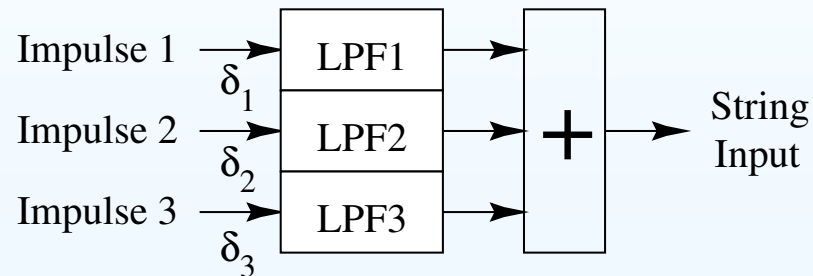
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Multiple Hammer-String Interaction Pulses

Superimpose several individual pulses:



As impulse amplitude grows (faster hammer strike), output pulses become *taller and thinner*, showing less overlap.





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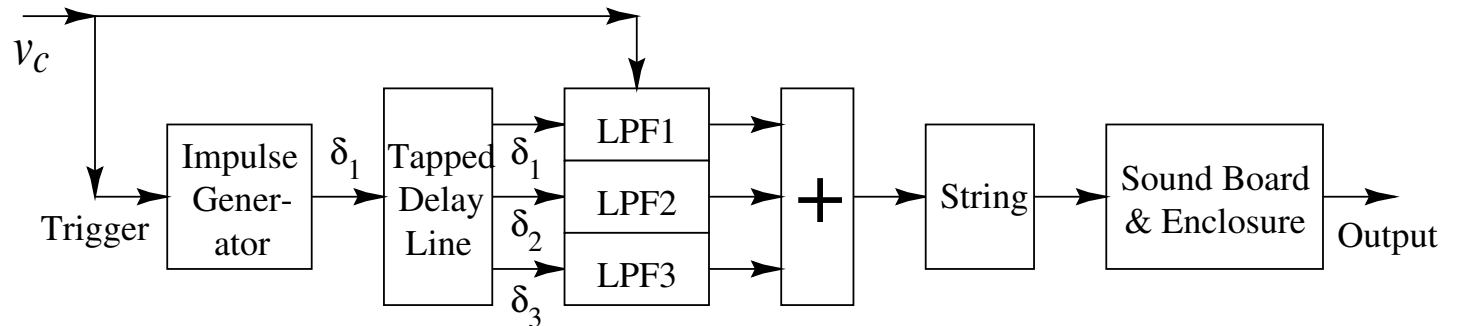
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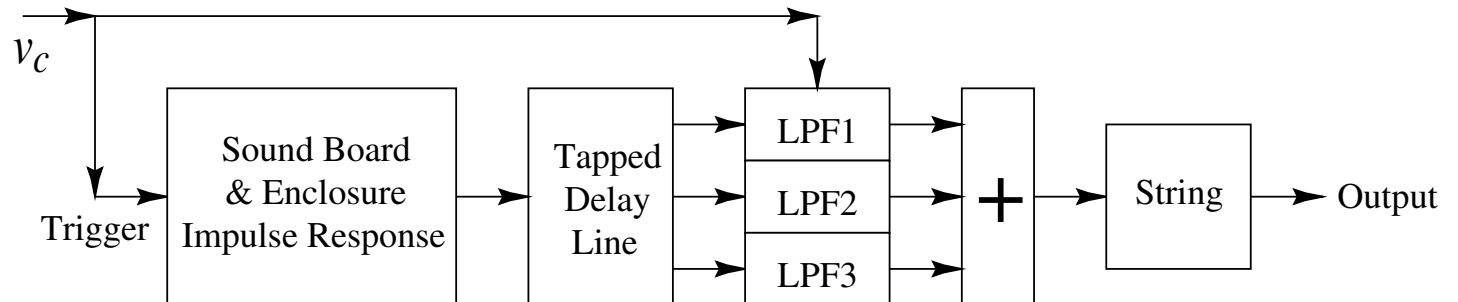
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Complete Piano Model

Natural Ordering:



Commuted Ordering:



- Soundboard and enclosure are *commuted*
- Only need a stored recording of their *impulse response*
- An enormous digital filter is otherwise required





Piano and Harpsichord Sound Examples

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(Stanford Sondius Project, ca. 1995)

- Piano: (WAV) (MP3)
- Harpsichord 1: (WAV) (MP3)
- Harpsichord 2: (WAV) (MP3)





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Summary

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More Recent Harpsichord Example

- Harpsichord Soundboard Hammer-Response: (WAV) (MP3)
- Musical Commuted Harpsichord Example: (WAV) (MP3)

Reference:

“Sound Synthesis of the Harpsichord Using a Computationally Efficient Physical Model”,

by Vesa Välimäki, Henri Penttinen, Jonte Knif, Mikael Laurson, and Cumhur Erkut

JASP-2004

Google search: *Harpsichord Sound Synthesis*





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Summary

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Physical Modeling in Audio Coding

Spectral modeling synthesis is finding application in audio coding.
Can physical modeling synthesis be used as well?

- MPEG-4/SAOL already supports essentially all sound synthesis methods
- Ability to *encode* sounds *automatically* is limited
 - Codebook-Excited Linear Prediction (CELP) is a successful *source-filter* model (not quite physical)
 - There are many isolated examples of model-fitting to recorded data
 - Good *model-based denoising* results have been obtained
 - Coder problem much harder when many sources are mixed





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- **Phy Audio Coding**
- Phy Audio Coding?

Summary

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Best Known Model-Based Audio Coders

A “cover band” can put together a very convincing facsimile of popular music performance



JOS high-school band “Bittersweet”





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- **Phy Audio Coding?**

Summary

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Future Physical Modeling in Audio Coding?

A “Cover Band” Approach to Model-Based Audio Coding:

1. Recognize individual “audio streams” in a mix (CASA)
(*“I hear a trap set, electric bass, Fender Rhodes, and a strat”*)
2. For each stream, calibrate its model heuristically
(*“Here is what I hear the bass part doing: ...”*)
3. Fine-tune the synthetic mix to the real mix
(joint “maximum likelihood estimation”)

Features of “Cover-Band Coding” (CBC):

- The “playing experience” of each “virtual performer” prevents artifacts — “musically unreasonable” parameters are made unlikely (“Bayesian priors”)
- An incorrect instrument must “imitate” its assigned stream
- New arrangements can be synthesized by deliberately choosing a new ensemble!





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Summary

We have reviewed a “CCRMA-centric slice” of the history of digital sound synthesis (usually starting with results from Bell Labs):

- Wavetable (one period)
- Subtractive
- Additive
- FM
- Sampling
- Spectral Modeling
- Physical Modeling (more in tomorrow’s 4:30 PM masterclass)
- Connections to audio coding



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Sound Acknowledgment

Thanks to Emu / Creative Labs for providing a superb-quality *external D/A converter* for this talk (an E-Mu 0404/USB)